

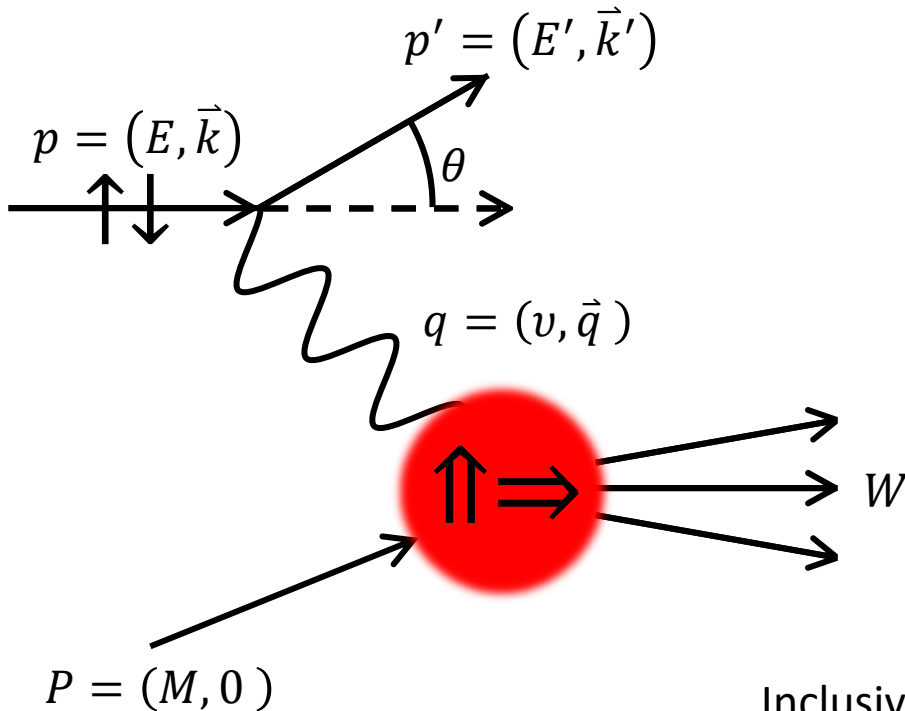
A Measurement of the g_2 Spin Structure Function at Low Q^2



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APS 2016 Salt Lake City, Utah



Inclusive Electron Scattering



Inclusive unpolarized cross section:

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_{Mott} \left[\frac{1}{\nu} F_2(x, Q^2) + \frac{2}{M} F_1(x, Q^2) \tan^2\left(\frac{\theta}{2}\right) \right]$$

Inclusive polarized cross section differences:

$$\frac{d^2\sigma}{d\Omega dE'} (\uparrow\uparrow - \downarrow\uparrow) = \frac{4\alpha^2}{MQ^2\nu} \frac{E'}{E} \left[(E + E' \cos \theta) g_1(x, Q^2) - \frac{Q^2}{\nu} g_2(x, Q^2) \right]$$

$$\frac{d^2\sigma}{d\Omega dE'} (\uparrow\Rightarrow - \downarrow\Rightarrow) = \frac{4\alpha^2 \sin \theta}{MQ^2\nu^2} \frac{E'^2}{E} [\nu g_1(x, Q^2) - 2E g_2(x, Q^2)]$$

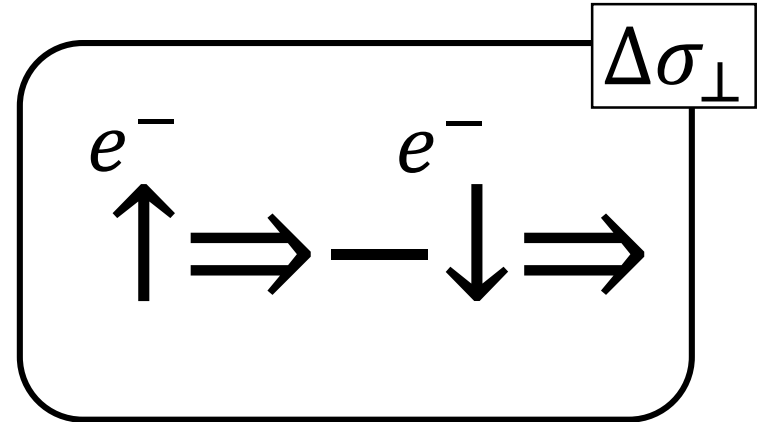
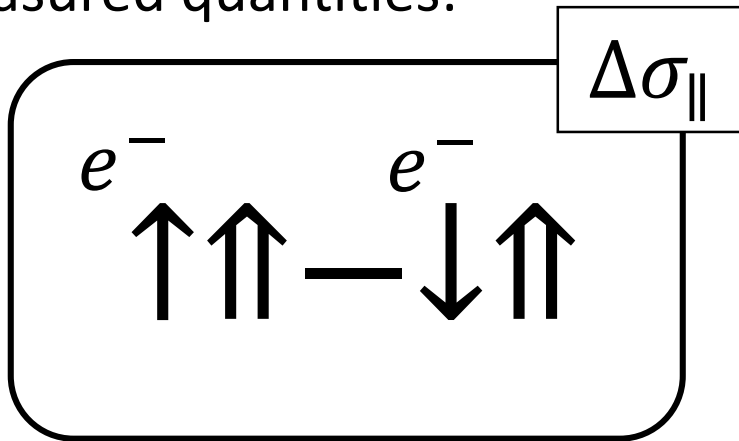
$$Q^2 = -q^2 = 4EE' \sin^2\left(\frac{\theta}{2}\right)$$

$$W^2 = M^2 + 2M\nu - Q^2$$

$$x = \frac{Q^2}{2M\nu}$$

Experimental Technique

Measured quantities:



$$g_1 = \frac{MQ^2}{4\alpha_e^2} \frac{y}{(1-y)(2-y)} \left[\Delta\sigma_{\parallel} + \tan\frac{\theta}{2} \Delta\sigma_{\perp} \right]$$

$\Delta\sigma_{\perp}$ contributes only $\sim 5\%$ to g_1 at our kinematics.

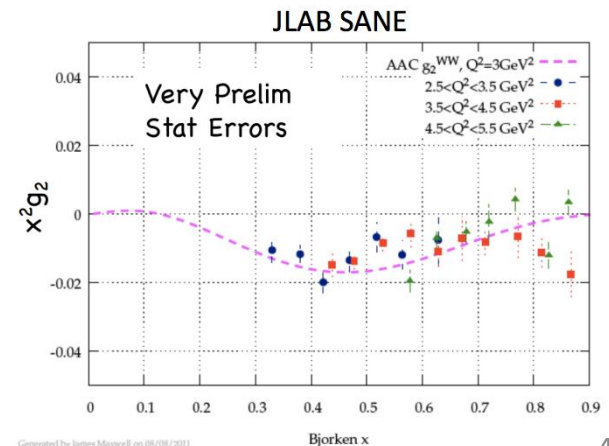
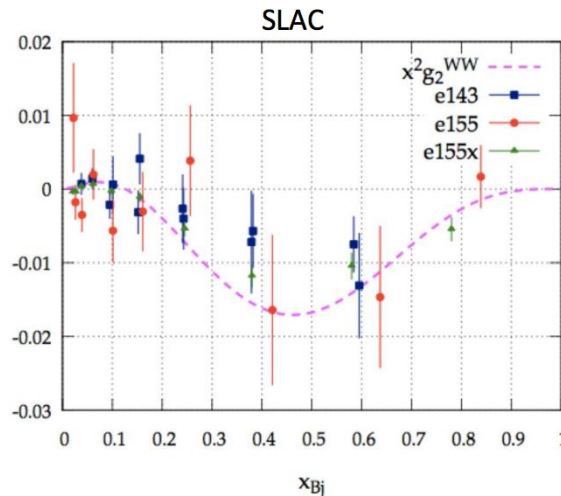
$$g_2 = \frac{MQ^2}{4\alpha_e^2} \frac{y^2}{2(1-y)(2-y)} \left[-\Delta\sigma_{\parallel} + \frac{1 + (1-y) \cos\theta}{(1-y) \sin\theta} \Delta\sigma_{\perp} \right]$$

$\Delta\sigma_{\perp}$ measured during g_2^p experiment, $\Delta\sigma_{\parallel}$ contributes $\sim 2 - 8\%$ to g_2 .

Motivation

- Very little data exists for the proton g_2 structure function.
- Measurements at Jefferson Lab:
 - RSS ($1 < Q^2 < 2 \text{ GeV}^2$) **published**
 - SANE ($2 < Q^2 < 6 \text{ GeV}^2$) **analysis**
 - g2p ($0.02 < Q^2 < 0.2 \text{ GeV}^2$) **analysis**
- A low Q^2 measurement will be a useful tool for testing the validity of χ PT and the moments of g_2 .

Existing data:



Generated by James Mainwaring on 06/06/2011

The B.C. Sum Rule

- 0^{th} moment of g_2 :

$$\Gamma_2 = \int_0^1 g_2(x, Q^2) dx = 0$$

- Existing data:

Brown: SLAC E155x

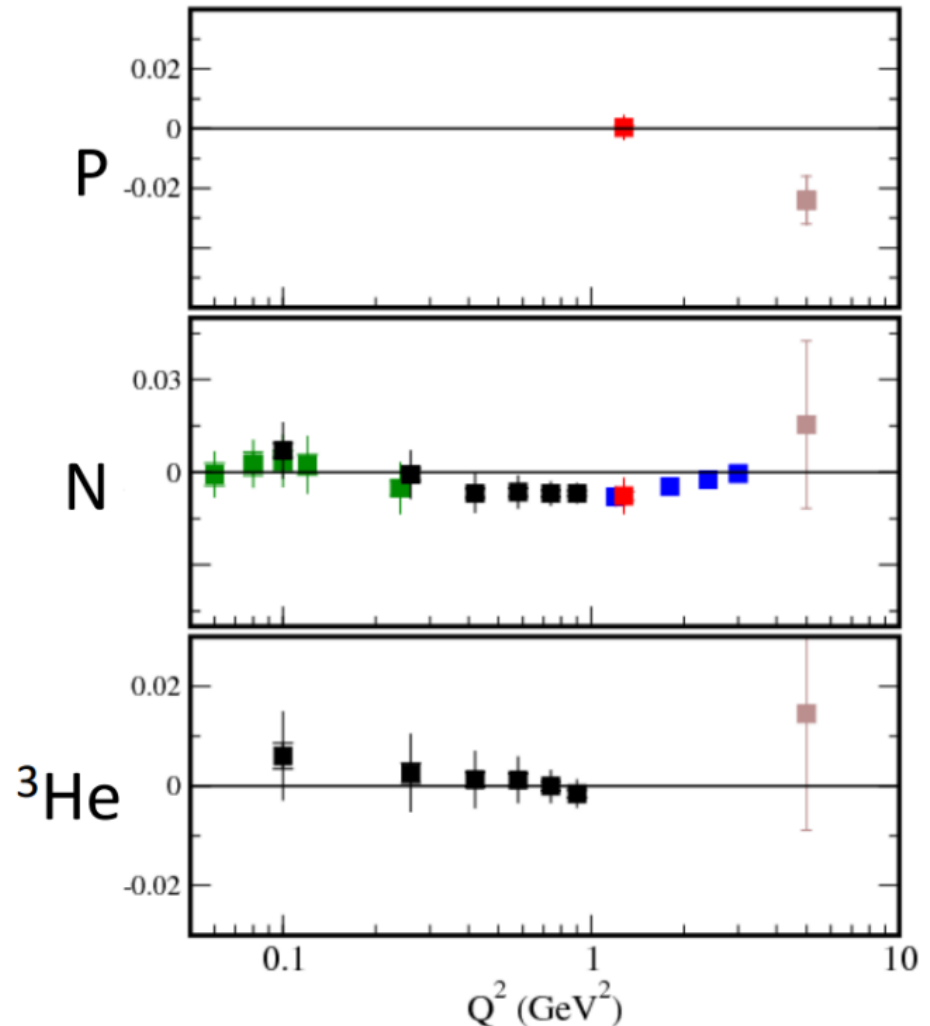
Red: Hall C RSS

Black: Hall A E94-010

Green: Hall A E97-110

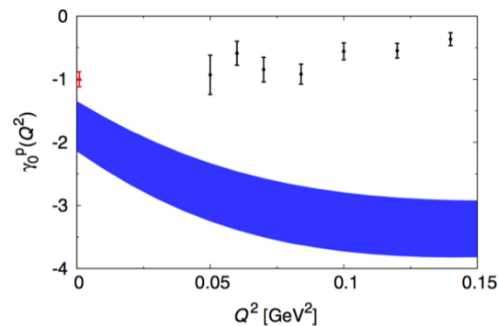
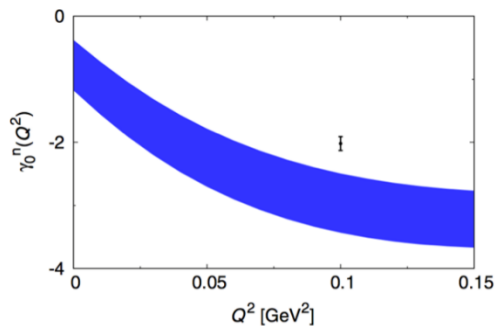
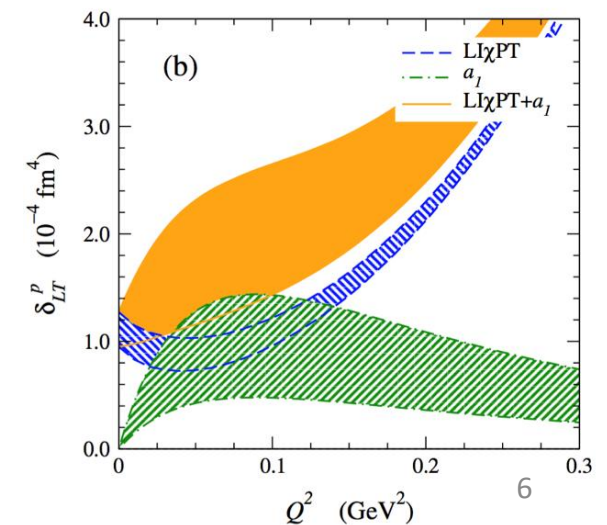
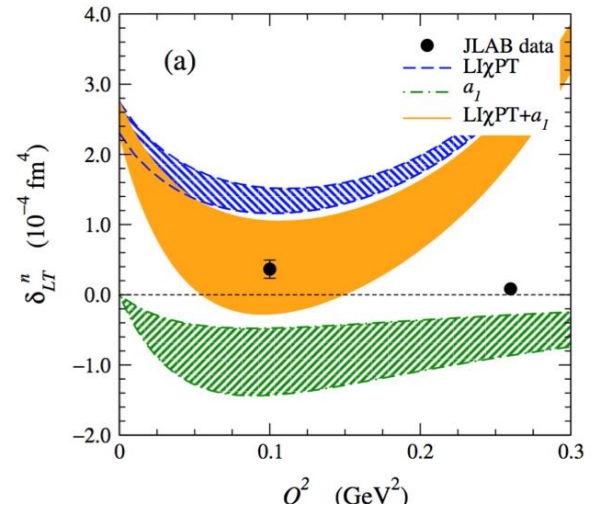
Blue: Hall A E01-012

- G2p hopes to fill in low Q^2 region for the proton.

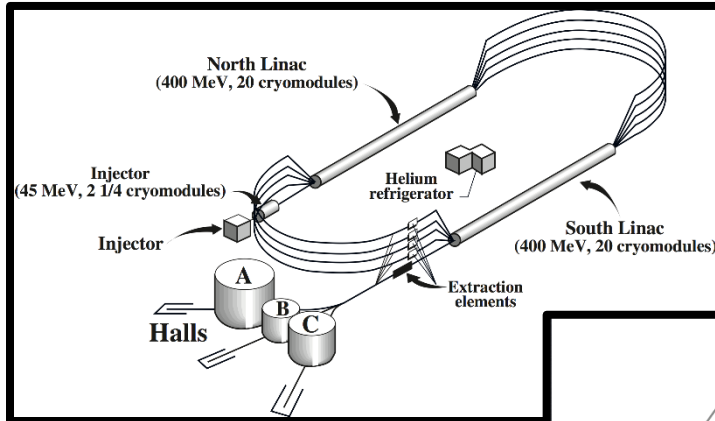


Spin Polarizabilities

- $\gamma_o = \frac{16\alpha M^2}{Q^6} \int_0^{x_o} x^2 \left[g_1(x, Q^2) - \frac{4M^2}{Q^2} x^2 g_2(x, Q^2) \right] dx$
- $\delta_{LT} = \frac{16\alpha M^2}{Q^6} \int_0^{x_o} x^2 [g_1(x, Q^2) + g_2(x, Q^2)] dx$
- Generalized spin polarizabilities γ_o and δ_{LT} are benchmark tests of χ PT.
- Some disagreement with neutron polarizabilities.
- No proton data yet!



Experimental Setup

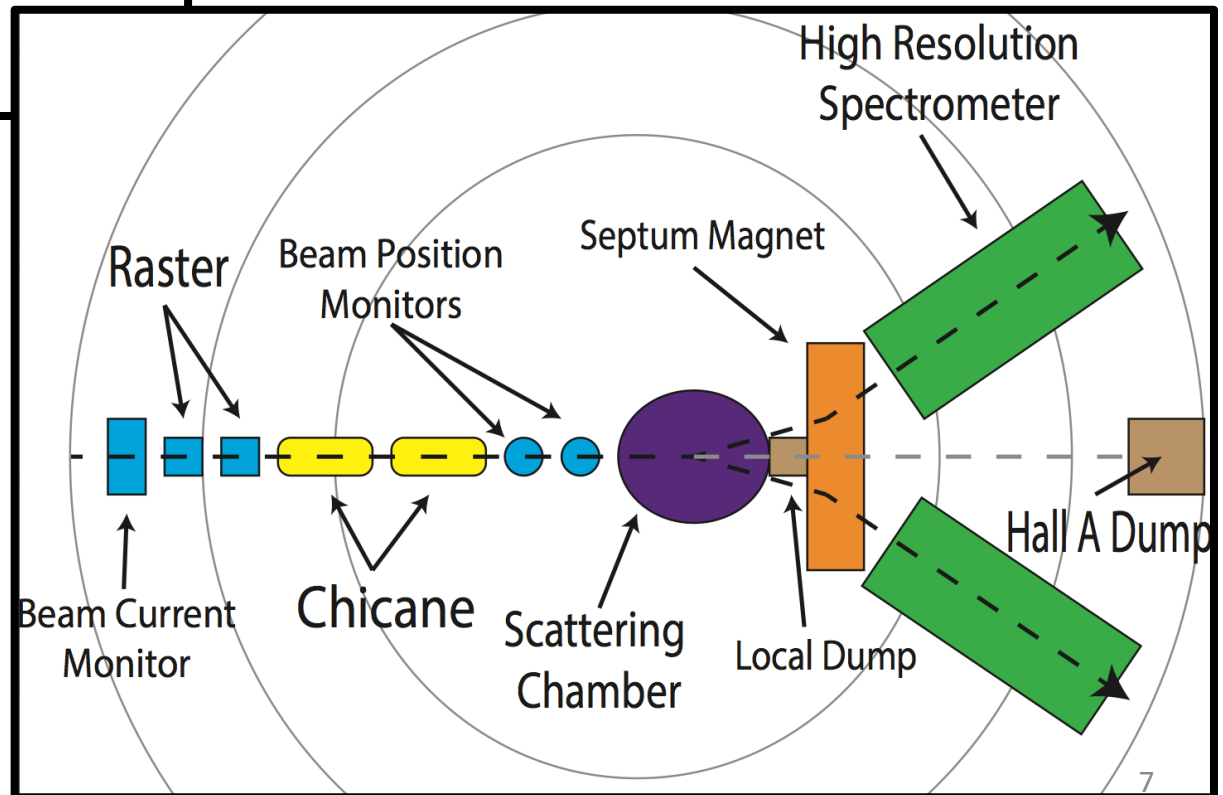


Jefferson Lab CEBAF:

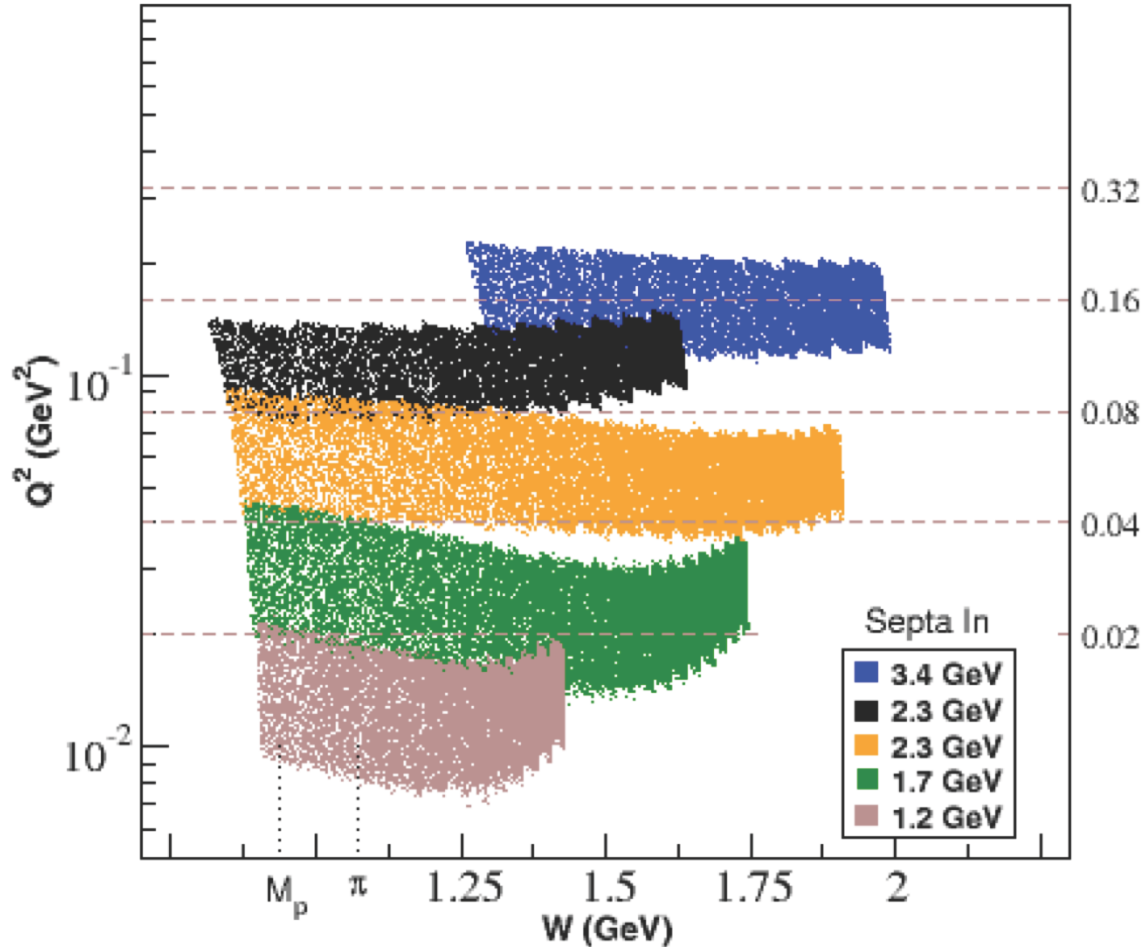
- 12 GeV maximum beam energy
- 200 μA maximum current
- 85% electron polarization

Hall A:

- All new beam diagnostics (BPM, BCM, rasters)
- Chicane installed for transverse target field
- 2.5/5T rotatable target field
- Septum magnet for small scattering angles



Kinematic Coverage



Beam Energy (GeV)	Target Field (T)
3.352	5
2.254	5
2.254	2.5
1.706	2.5
1.158	2.5

Model estimated kinematic coverage

Dilution and Packing Fraction

- The physics asymmetry first requires the calculation of two target quantities:

- The length ratio of material in the target cup, called the *packing fraction*.

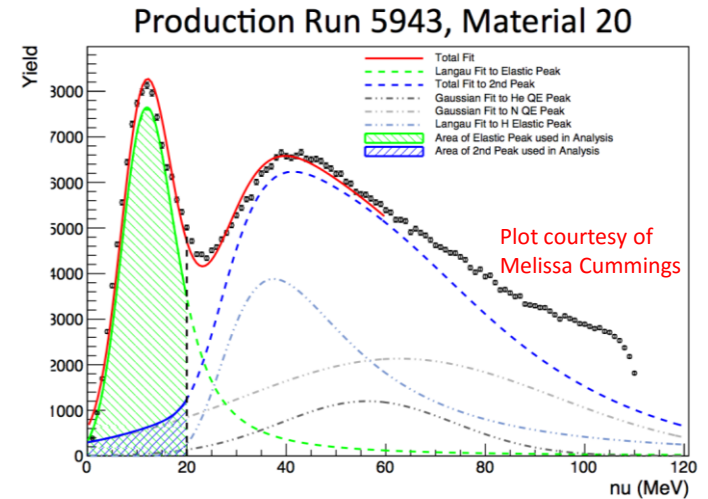
$$Pf = \left(\frac{Y_p}{Y_E} - 1 \right) \left(\frac{\chi_N \sigma_N + \chi_H \sigma_H}{\chi_{He} \sigma_{He}} \right)^{-1}$$

- The fractional composition of proton material in the target, called the *dilution factor*.

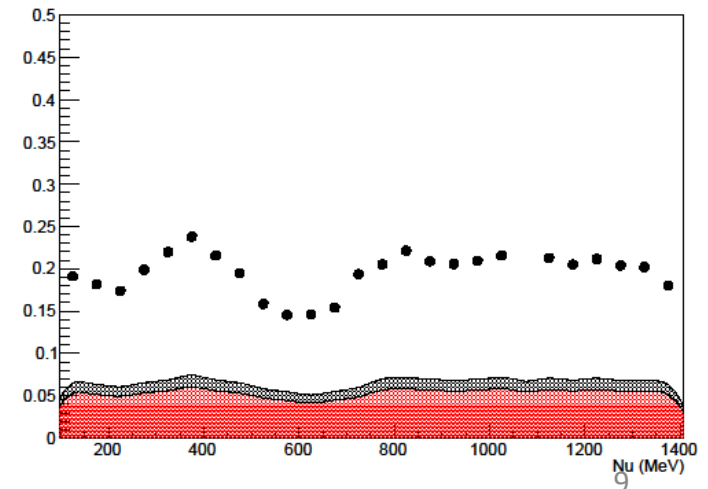
$$f = 1 - \frac{Y_{BG}}{Y_P}$$

- The asymmetry is then calculated as:

$$A_{phy} = \frac{1}{f P_b P_t} \frac{Y_+ - Y_-}{Y_+ + Y_-}$$



2.254GeV 5T Transverse Dilution

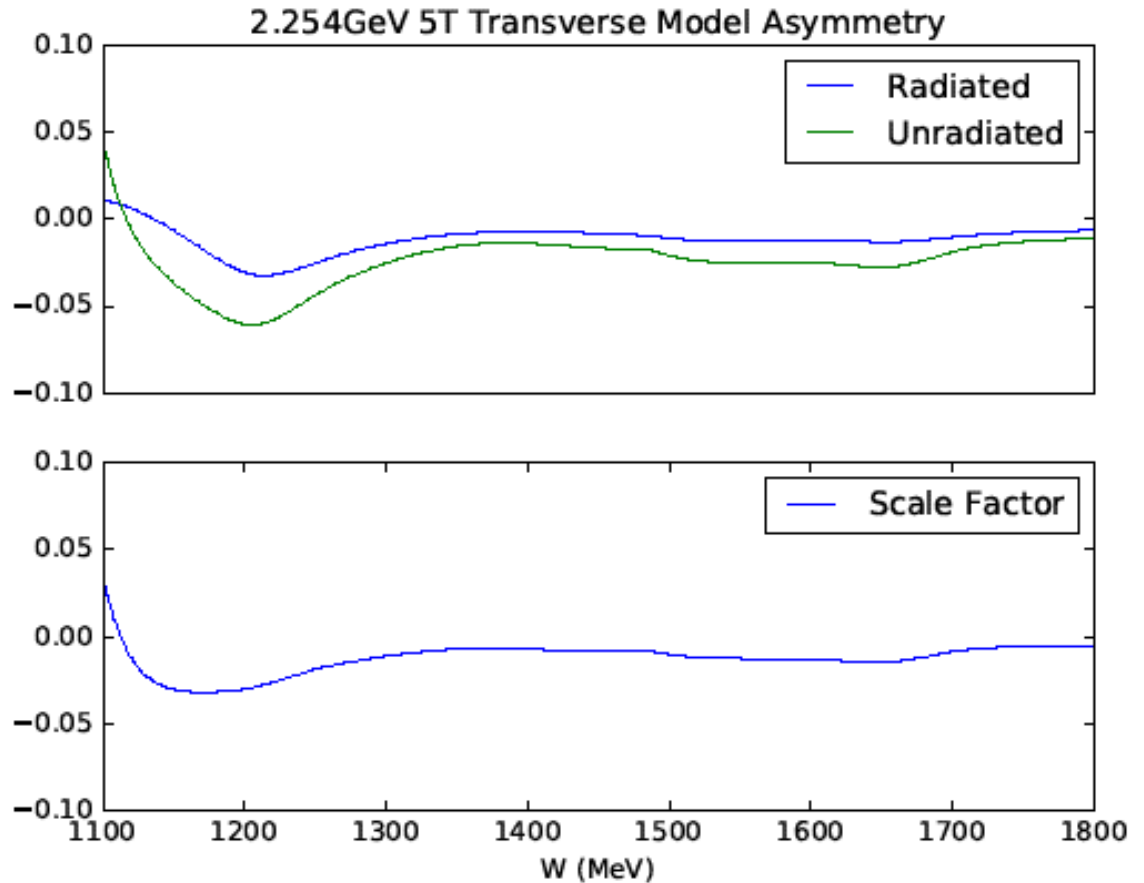


Radiative Corrections

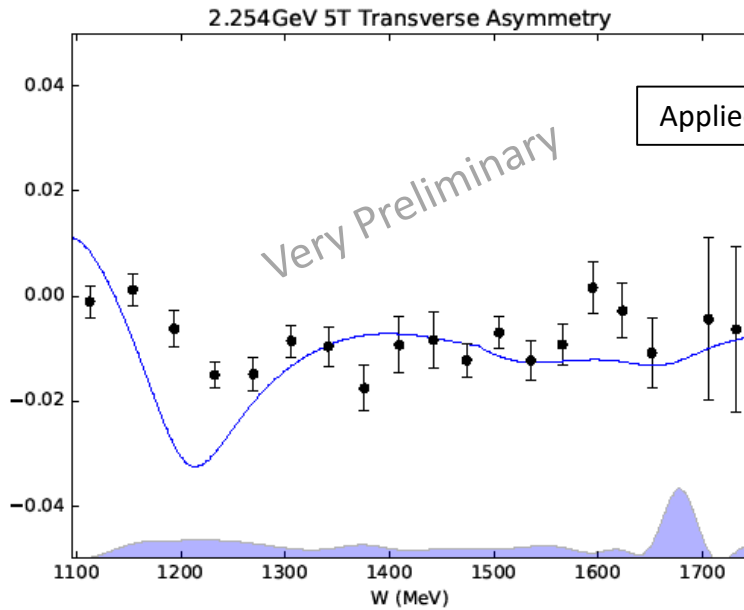
- Preliminary polarized radiative correction:

$$R = A_{unrad} - A_{rad}$$

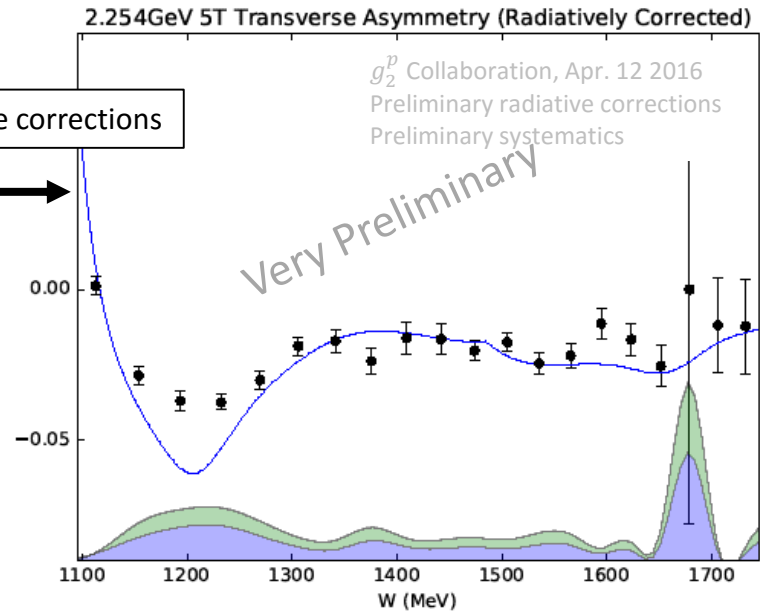
- $A_{(un)rad}$ is generated from MAID.
- Polarized radiative correction study is still underway, results will be updated when complete.



Physics Asymmetry



Applied radiative corrections



Preliminary systematics:

Target Polarization	2%
Inelastic XS Model	10%
Packing Fraction	45%
MAID	40%
Radiative correction	10%

Unpolarized Cross Section

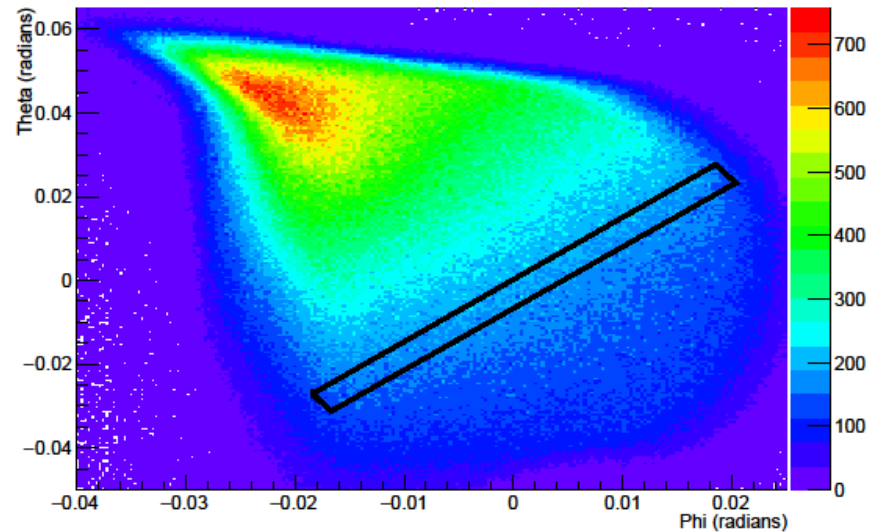
- Acceptance correction study is still underway.
- An acceptance cut is chosen such that the theta/phi distribution is flat within the cut region.
- Proton XS is calculated as:

$$\frac{d\sigma}{d\Omega dE} = \frac{eM_{NH_3}}{A\rho_{NH_3}Z_{NH_3}} fY_{NH_3}$$

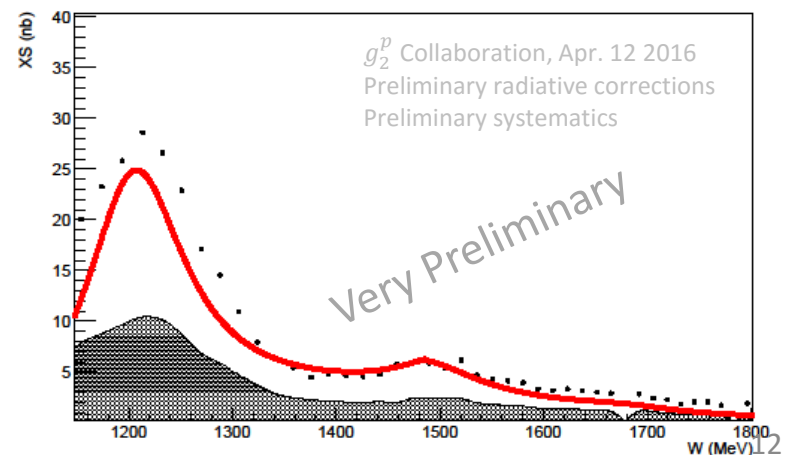
Preliminary systematics:

Unpolarized XS model	10%
Packing Fraction	45%
Unpolarized XS model (dilution)	10%

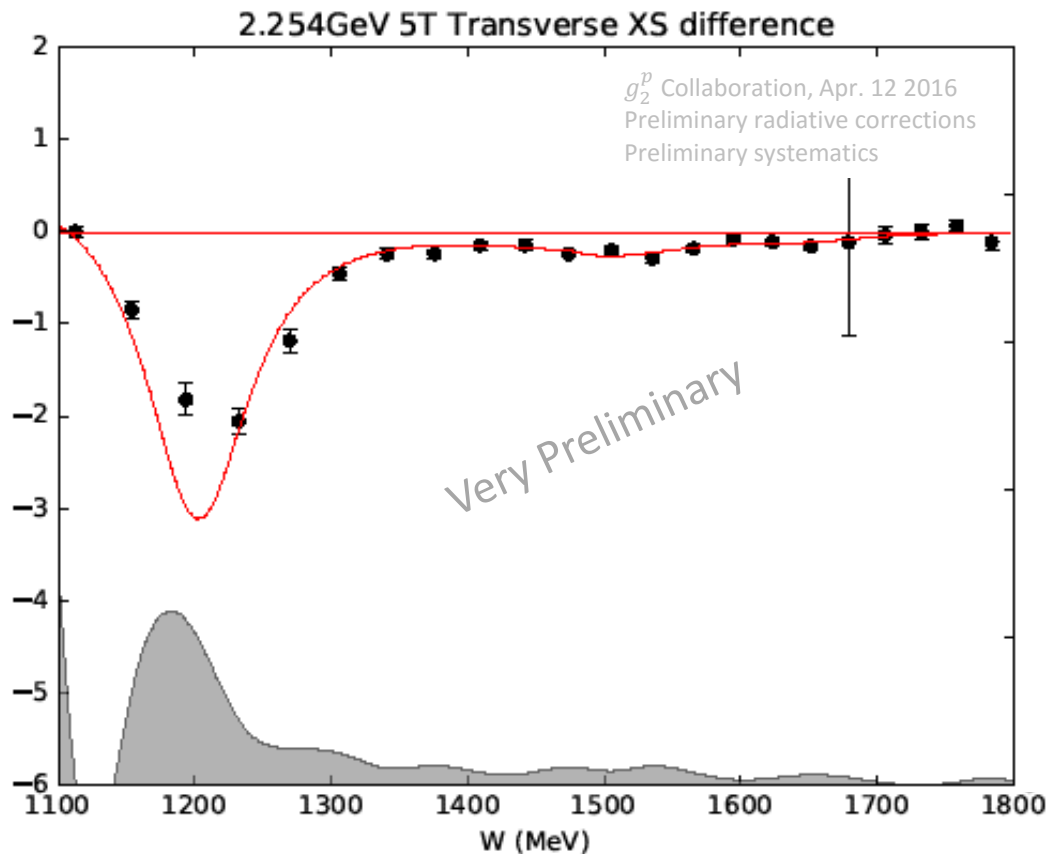
2.254GeV 5T Transverse Acceptance



2.254GeV Proton XS (Radiatively Corrected)



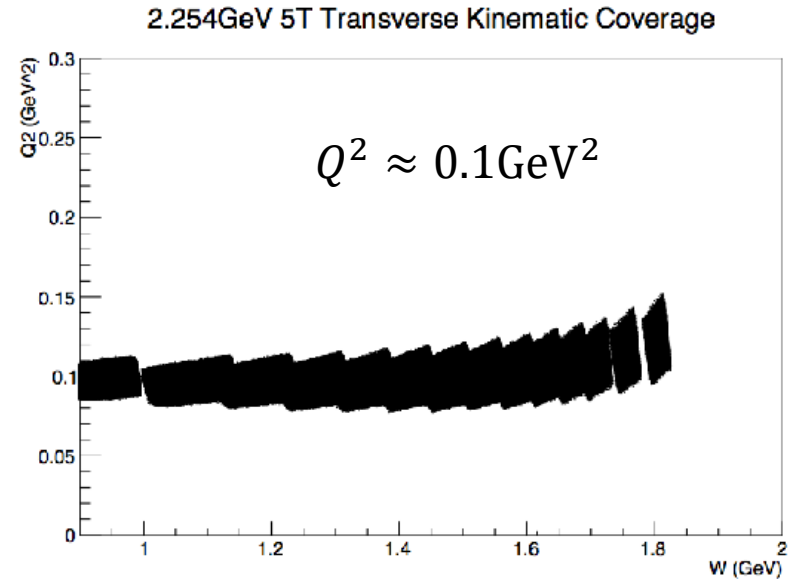
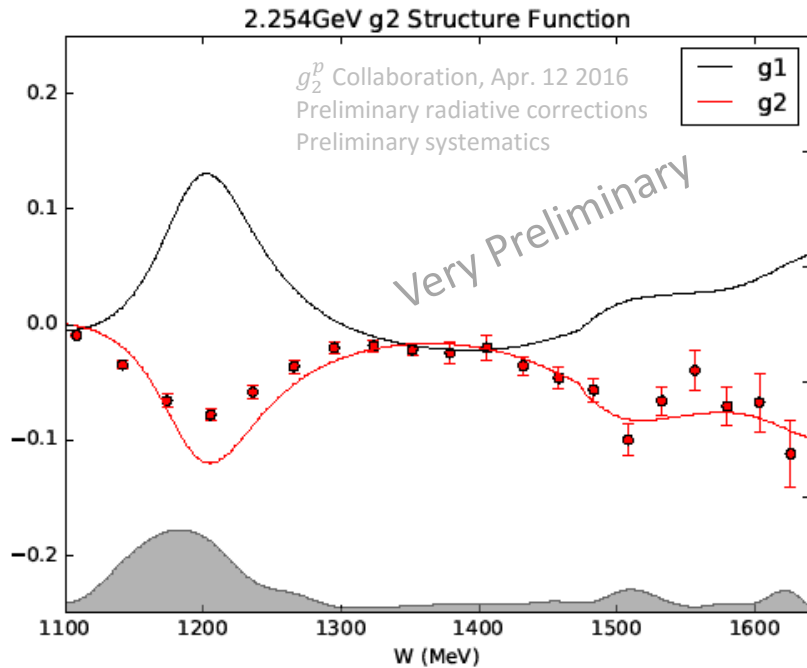
Cross Section Differences



Preliminary systematics:

Unpolarized XS model	10%
MAID	40%
Target polarization	3%
Acceptance	25%

Proton Spin Structure Functions



Preliminary systematics:

Unpolarized XS model	10%
MAID	40%
Target polarization	3%
Acceptance	25%

Summary

- A measurement of the proton spin structure function g_2 at low Q^2 is an important component in the testing of a number of effective theories of QCD.
- The g2p experiment, which measured g_2 in a Q^2 region of 0.02 – 0.2 GeV², successfully ran at Jefferson Lab during the spring of 2012 and analysis is still ongoing.
- Preliminary methods for determining the acceptance and radiative effects give promising results for the spin structure at a Q^2 of 0.1 GeV².
- Current efforts are focused on improving these methods and reducing systematics.
- More results to come shortly!

Thank You!

G2p Analysis Team:

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