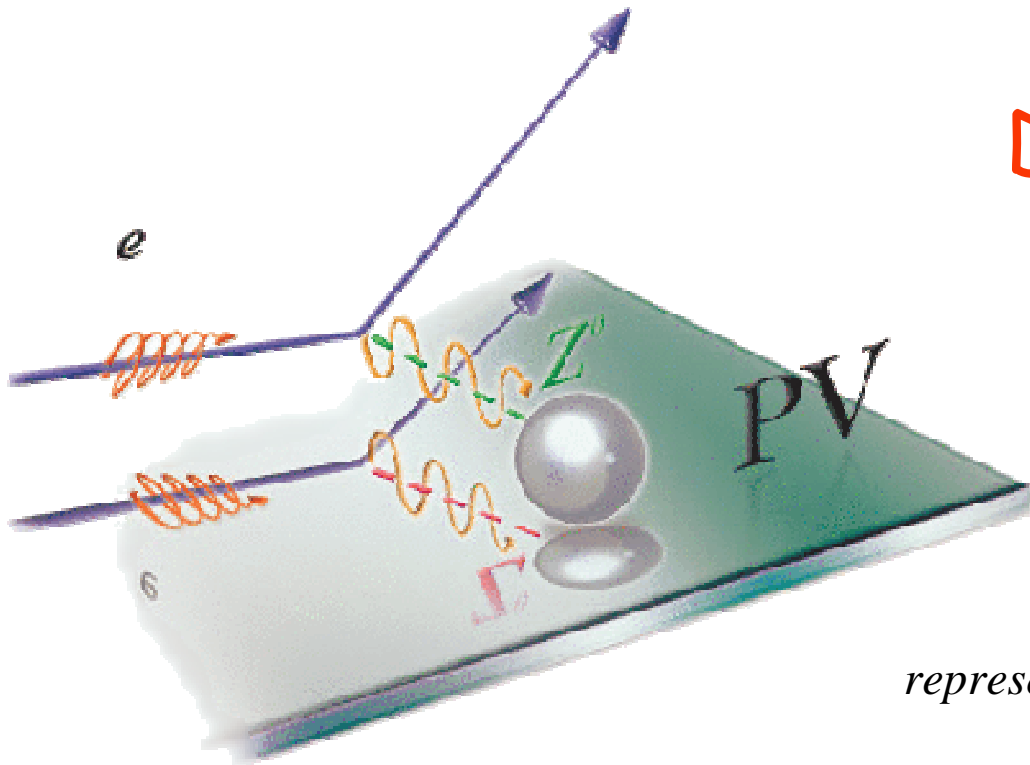


New Results from the HAPPEX Experiments at $Q^2 = 0.1 \text{ GeV}/c^2$

David S. Armstrong

College of William & Mary



representing the **HAPPEX Collaboration**

From Parity Violation to Hadronic Structure... (PAVI 2006) Milos, Greece May 16 2006



The College of
WILLIAM & MARY



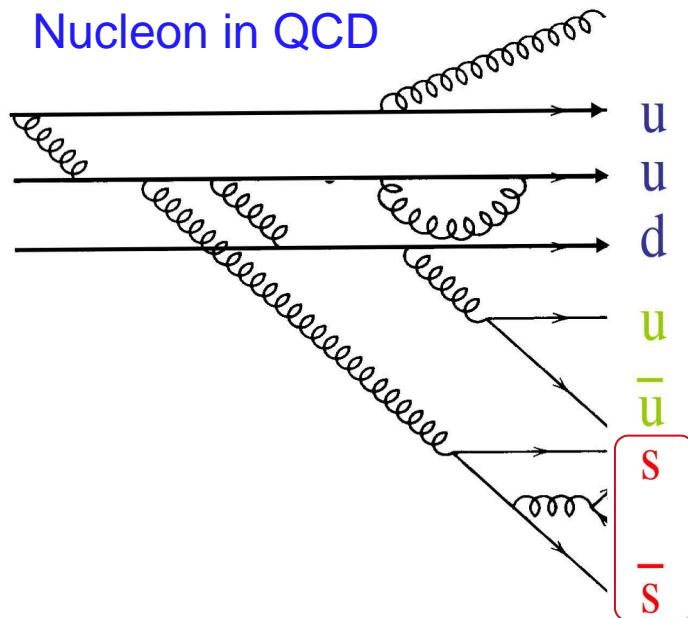
Outline

- Parity-violation in electron scattering
- Elastic Vector Strange Form Factors: G_E^s and G_M^s
- $Q^2 = 0.1 \text{ (GeV/c)}^2$ as/of early 2005
- Latest results from HAPPEX-II:
 - HAPPEX-hydrogen and HAPPEX-Helium
- The present situation at $Q^2 = 0.1 \text{ (GeV/c)}^2$
- Implications and Conclusions

"There is no excellent beauty that hath not some strangeness in the proportion"

Francis Bacon 1561-1626

Strangeness in the nucleon



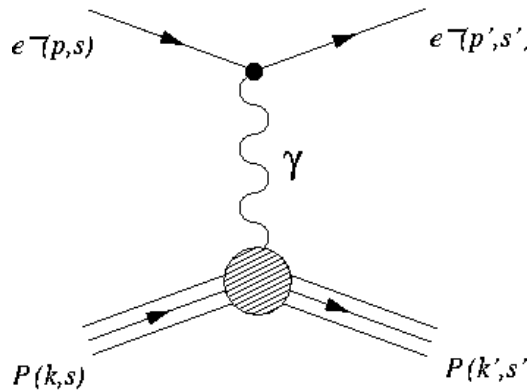
- $P = uud + \underbrace{u\bar{u} + d\bar{d} + s\bar{s} + g + \dots}_{\ll \text{sea} \gg}$

- s quark: cleanest candidate to study the sea
-) How much do virtual $s\bar{s}$ pairs contribute to the structure of the nucleon ?
 - Momentum : 4 % (DIS)
 - Spin : 0 to -10% (polarized DIS)
 - Mass : 0 to 30 % (πN -sigma term)
 (large uncertainties on these contributions)

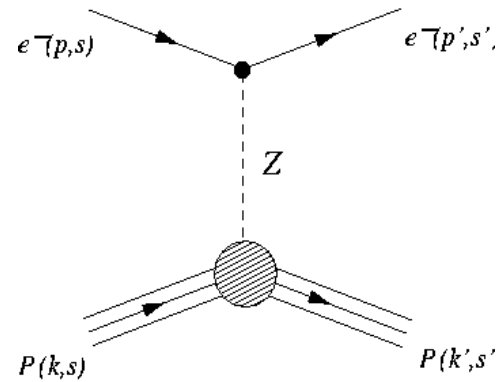
Goal: Determine the contributions of the strange quark sea ($s\bar{s}$) to the charge and current/spin distributions in the nucleon :

“strange form factors” G_E^s and G_M^s

Parity Violating Electron Scattering → Weak NC Amplitudes



$$M^{EM} = \frac{4\pi\alpha}{Q^2} Q_\ell \ell^\mu J_\mu^{EM}$$



$$M_{PV}^{NC} = \frac{G_F}{2\sqrt{2}} [g_A \ell^{\mu 5} J_\mu^{NC} + g_V \ell^\mu J_{\mu 5}^{NC}]$$

Interference: $\sigma \sim |M^{EM}|^2 + |M^{NC}|^2 + 2\text{Re}(M^{EM*})M^{NC}$

Interference with EM amplitude makes Neutral Current (NC) amplitude accessible

$$\Rightarrow A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \sim \frac{|M_{PV}^{NC}|}{|M^{EM}|} \sim \frac{Q^2}{(M_Z)^2}$$

Tiny ($\sim 10^{-6}$) cross section asymmetry isolates weak interaction

Form Factors

$$J_{\mu}^{EM} = \sum_q Q_q \langle \bar{N} | \bar{u}_q \gamma_{\mu} u_q | N \rangle = \bar{N} \left[\gamma_{\mu} F_1^{\gamma} + \frac{i \sigma_{\mu\nu} q^{\nu}}{2M_N} F_2^{\gamma} \right] N$$

Adopt the Sachs FF: $G_E^{\gamma} = F_1^{\gamma} + \tau F_2^{\gamma}$ $G_M^{\gamma} = F_1^{\gamma} + F_2^{\gamma}$
(Roughly: Fourier transforms of charge and magnetization)

NC probes **same** hadronic flavor structure, with different couplings:

$$G_{E/M}^{\gamma} = \frac{2}{3} G_{E/M}^u - \frac{1}{3} G_{E/M}^d - \frac{1}{3} G_{E/M}^s$$

$$G_{E/M}^Z = \left(1 - \frac{8}{3} \sin^2 \theta_W \right) G_{E/M}^u - \left(1 - \frac{4}{3} \sin^2 \theta_W \right) G_{E/M}^d - \left(1 - \frac{4}{3} \sin^2 \theta_W \right) G_{E/M}^s$$

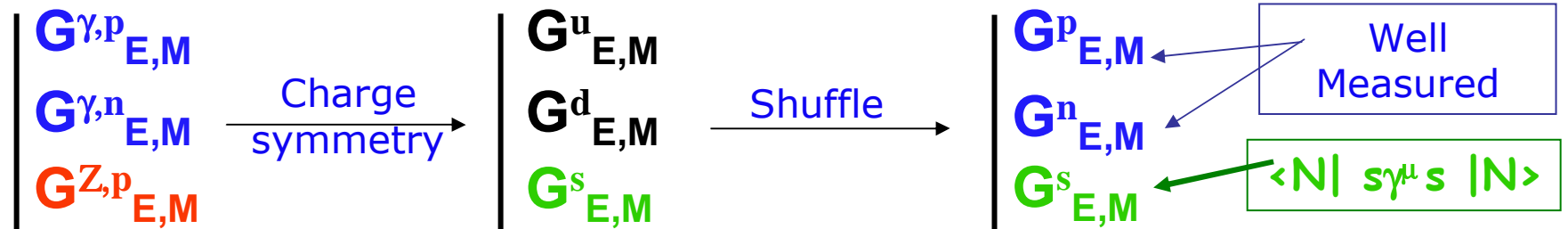
$G_{E/M}^Z$ provide an important new benchmark for testing non-perturbative QCD structure of the nucleon

Charge Symmetry

One expects the neutron to be an isospin rotation of the proton*:

$$G_{E/M}^{p,u} = G_{E/M}^{n,d}, \quad G_{E/M}^{p,d} = G_{E/M}^{n,u}, \quad G_{E/M}^{p,s} = G_{E/M}^{n,s}$$

$$G_{E/M}^{\gamma,p} = \frac{2}{3} G_{E/M}^u - \frac{1}{3} G_{E/M}^d - \frac{1}{3} G_{E/M}^s \quad \rightarrow \quad G_{E/M}^{\gamma,n} = \frac{2}{3} G_{E/M}^d - \frac{1}{3} G_{E/M}^u - \frac{1}{3} G_{E/M}^s$$



$$A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \propto \frac{M_Z M_\gamma}{|M_\gamma|^2} = -\frac{G_F Q^2}{\sqrt{2\pi\alpha}} F(G_{E/M}^p, G_{E/M}^n, G_{E/M}^s, G_A)$$

* See B. Kubis & R. Lewis [nucl-th/0605006](https://arxiv.org/abs/nuc-th/0605006) & Randy Lewis' talk at this meeting

Isolating the form factors:
vary the *kinematics* or *target*

For a proton:

$$A = \left[\frac{-G_F Q^2}{4\pi\alpha\sqrt{2}} \right] \frac{A_E + A_M + A_A}{\sigma_p} \quad \sim \text{few parts per million}$$

$$A_E = \epsilon G_E^p G_E^Z, \quad A_M = \tau G_M^p G_M^Z, \quad A_A = -(1 - 4 \sin^2 \theta_W) \epsilon' G_M^p G_A^e$$

Forward angle Backward angle

$$G_{E,M}^Z = (1 - 4 \sin^2 \theta_W)(1 + R_V^p)G_{E,M}^p - (1 + R_V^n)G_{E,M}^n - G_{E,M}^s$$

$$G_A^e = -G_A + \Delta s + \eta F_A + R^e$$

For ${}^4\text{He}$: G_E^s alone

$$A_{PV} = \frac{G_F Q^2}{\pi\alpha\sqrt{2}} \left[\sin^2 \theta_W + \frac{G_E^s}{2(G_E^p + G_E^n)} \right]$$

For deuterium:

enhanced G_A^e sensitivity

Theoretical Approaches to Strange Form Factors

Models - a non-exhaustive list:

kaon loops, vector dominance, Skyrme model, chiral quark model, dispersion relations, NJL model, quark-meson coupling model, chiral bag model, HBChPT, chiral hyperbag, QCD equalities, ...

- no consensus on magnitudes or even *signs* of G_E^s and G_M^s !

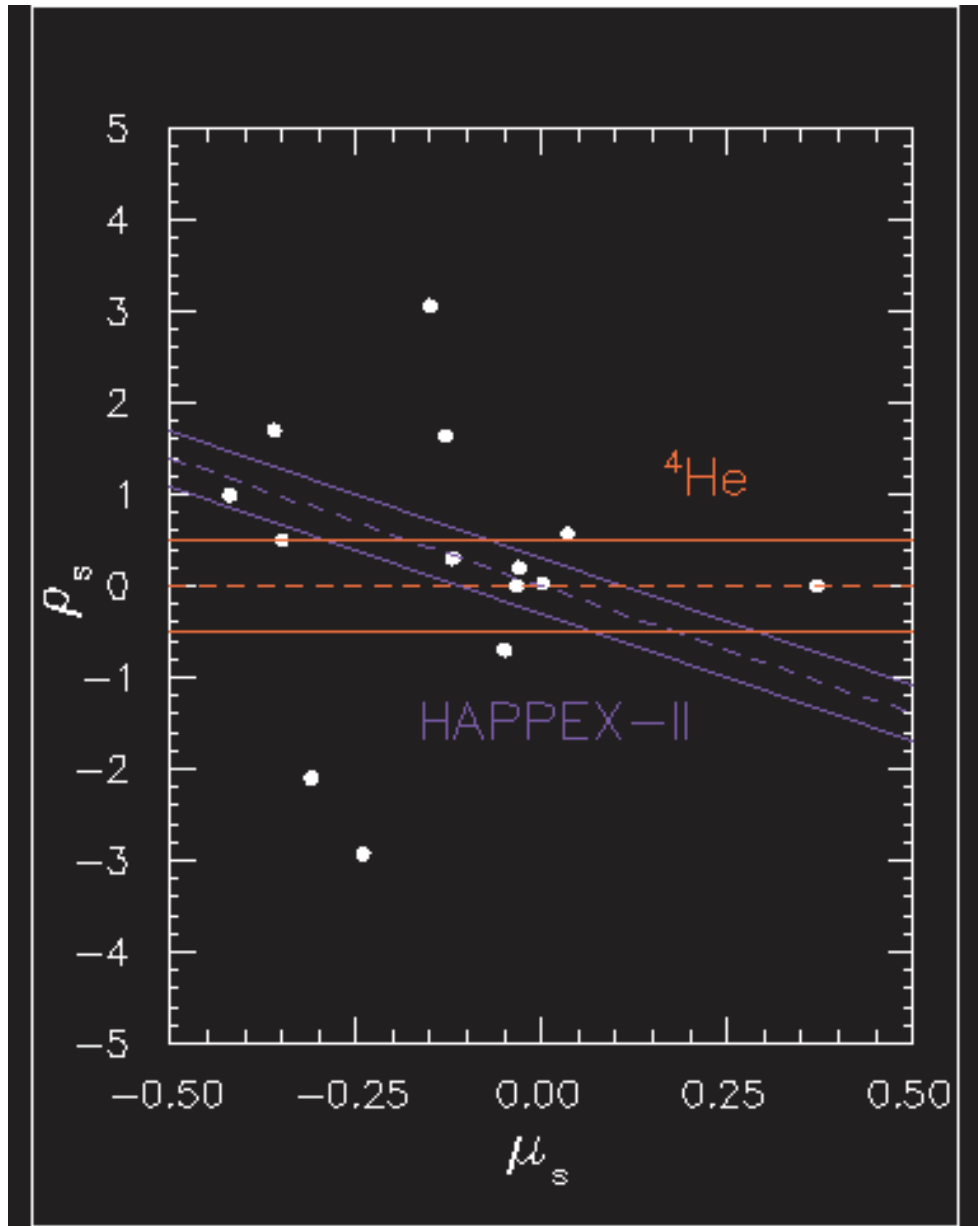
a challenging problem in non-perturbative QCD

What about QCD on the lattice?

- Dong, Liu, Williams PRD **58**(1998)074504
- Lewis, Wilcox, Woloshyn PRD **67**(2003)013003
- Leinweber, et al. PRL **94**(2005) 212001 *and* hep-lat/0601025

⇒ See Ross Young's talk

Strangeness Models (as/of 2000)



Leading moments of form factors:

$$\mu_s = G_M^s(Q^2=0)$$

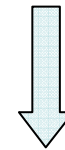
$$\rho_s = \partial G_E^s / \partial \tau (Q^2=0)$$

World Data (early 2005) at $Q^2 \sim 0.1 \text{ GeV}^2$

Note: SAMPLE result adopts
Zhu *et al.* calculation of G_A^e
PRD 62(2000)033008

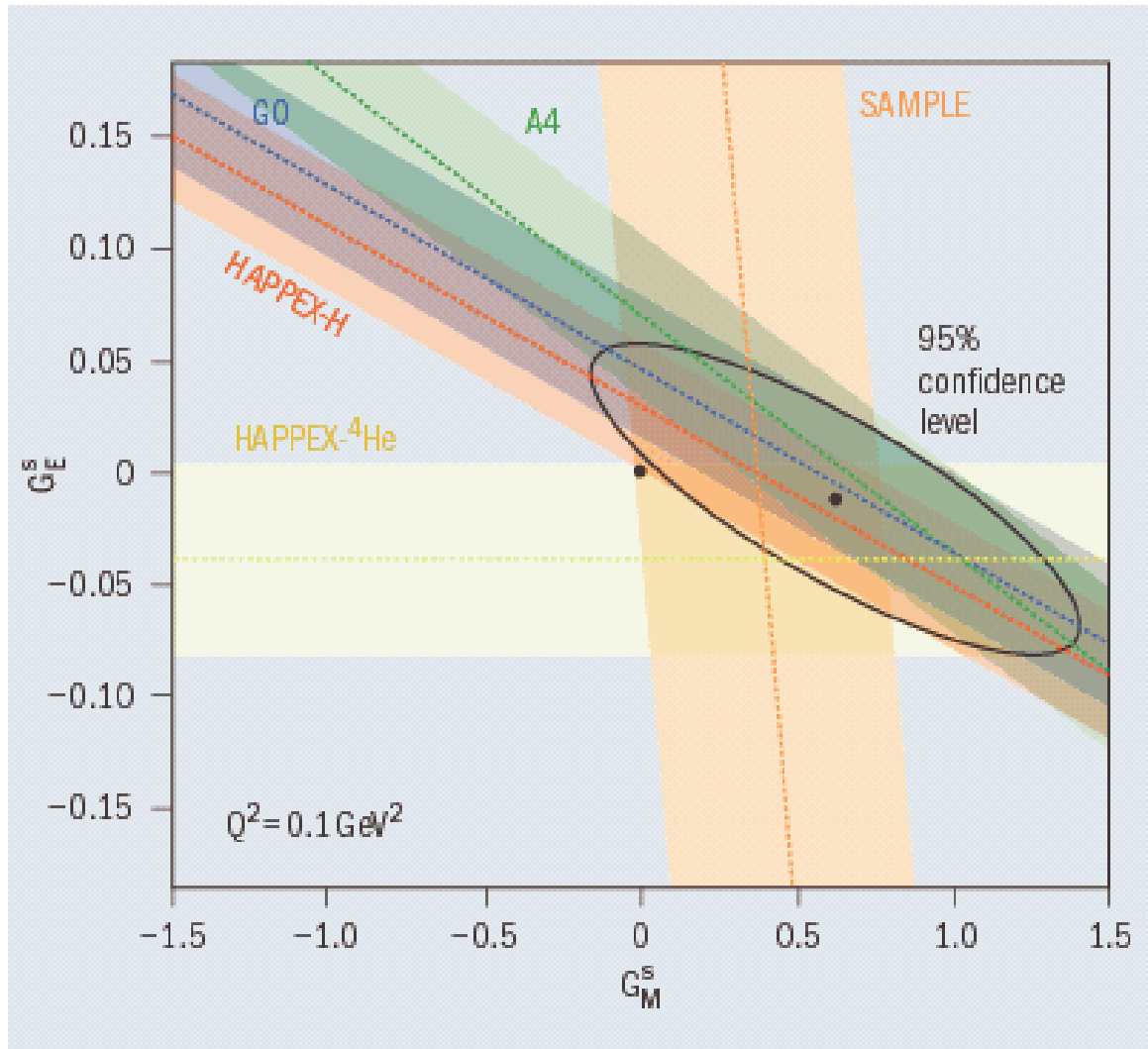
$$G_E^s = -0.12 \pm 0.29$$

$$G_M^s = 0.62 \pm 0.32$$



Would imply that 5-10%
of nucleon magnetic
moment is *Strange*

*Caution: the combined fit is
approximate. Correlated errors and
assumptions not taken into account*

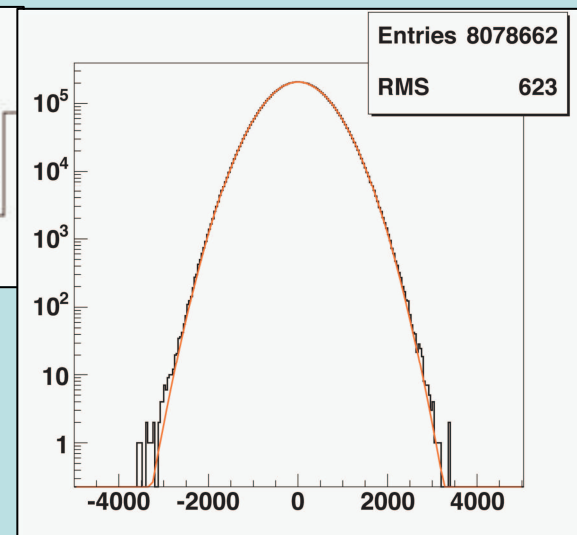
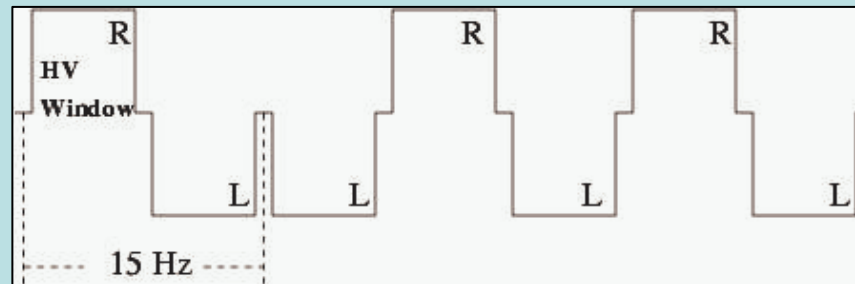


Measurement of P-V Asymmetries

$$A_{LR} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \approx 10^{-6} \quad \begin{array}{l} 5\% \text{ Statistical Precision on 1 ppm} \\ \rightarrow \text{requires } 4 \times 10^{14} \text{ counts} \end{array}$$

Rapid Helicity Flip: Measure the asymmetry at 10^{-4} level, 10 million times

$$A_{LR} = \frac{N_R - N_L}{N_R + N_L}$$



- High luminosity: thick targets, high beam current
- Control noise (target, electronics)
- High beam polarization and rapid flip

Statistics: high rate, low noise

Systematics: beam asymmetries, backgrounds, Helicity correlated DAQ

Normalization: Polarization, Linearity, Dilution

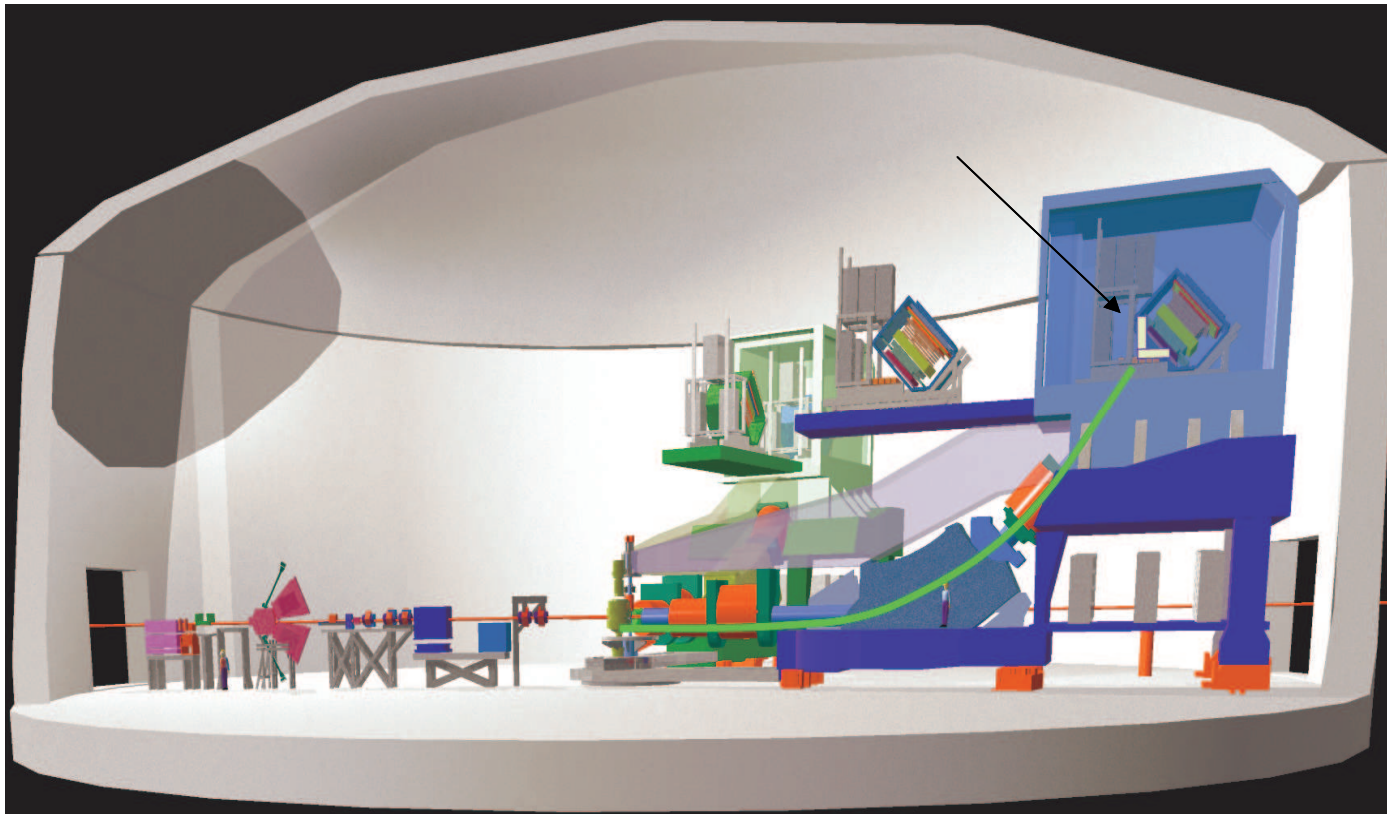
HAPPEX (second generation)

$$E=3 \text{ GeV} \quad \theta=6^\circ \quad Q^2=0.1 \text{ (GeV/c)}^2$$

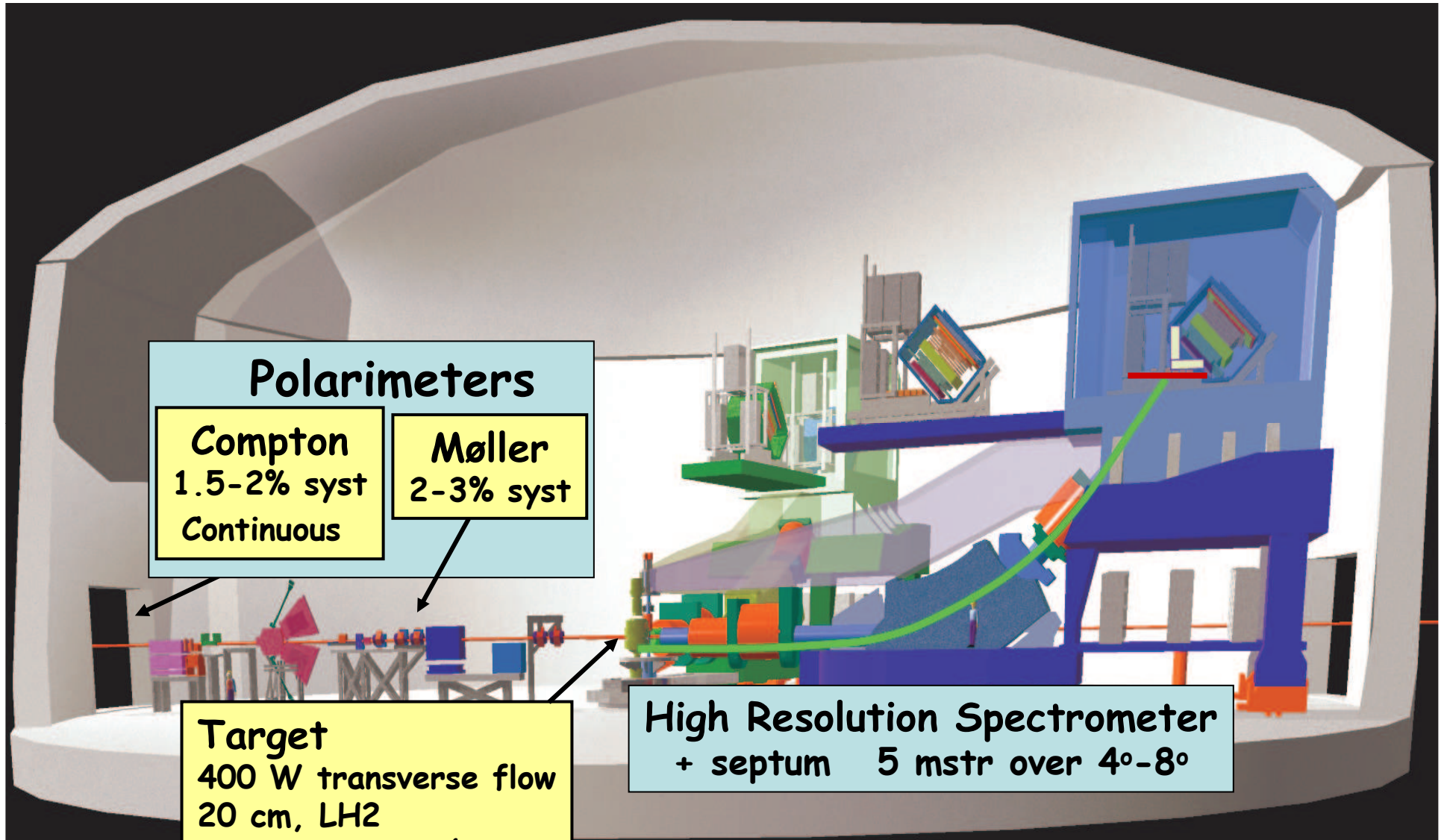
•Hydrogen : $G_E^s + \alpha G_M^s$

• ^4He : Pure G_E^s :
$$A^{PV} = -\frac{A_0}{2} \left(2 \sin^2 \theta_W + \frac{G_E^s}{G_E^{p\gamma} + G_E^{n\gamma}} \right)$$

New results: just released (P. Souder at Dallas APS meeting)



Hall A



Polarimeters

Compton 1.5-2% syst Continuous	Møller 2-3% syst
---	----------------------------

Target
400 W transverse flow
20 cm, LH2
20 cm, 200 psi ^4He

High Resolution Spectrometer
+ septum 5 mstr over 4° - 8°

Summary of Data Runs: HAPPEX-II

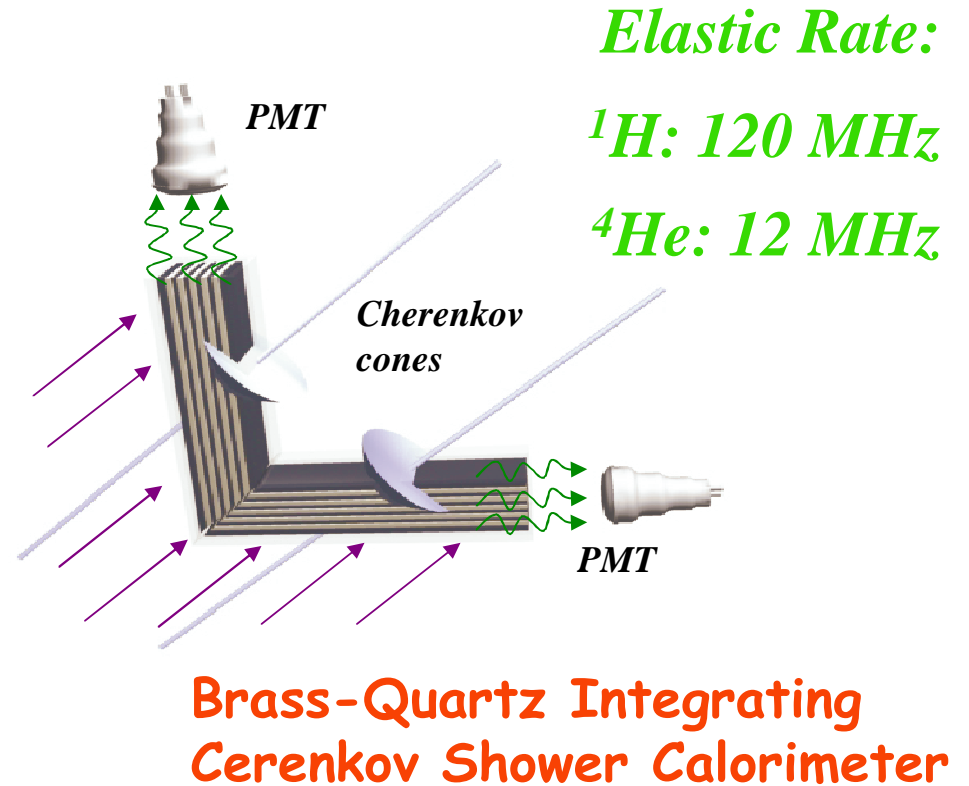
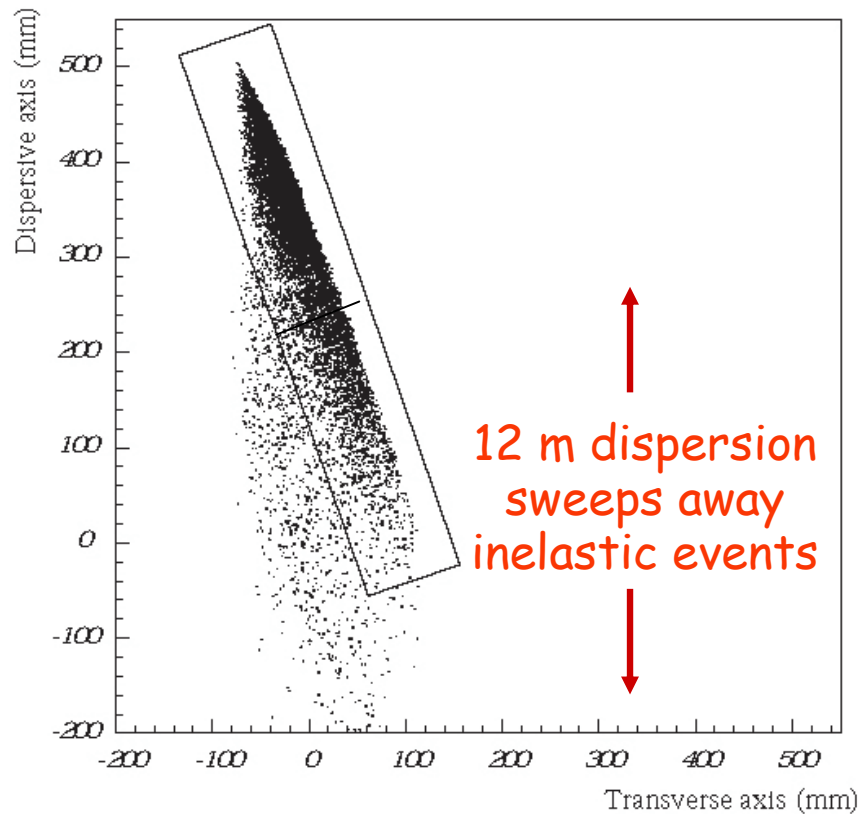
June 2004	HAPPEX-He <ul style="list-style-type: none">• about 3M pairs at 1300 ppm$\Rightarrow \delta A_{\text{stat}} \sim 0.74$ ppm
June - July 2004	HAPPEX-H <ul style="list-style-type: none">• about 9M pairs at 620 ppm$\Rightarrow \delta A_{\text{stat}} \sim 0.2$ ppm
July-Sept 2005	HAPPEX-He <ul style="list-style-type: none">• about 35M pairs at 1130 ppm$\Rightarrow \delta A_{\text{stat}} \sim 0.19$ ppm
Oct - Nov 2005	HAPPEX-H <ul style="list-style-type: none">• about 25M pairs at 540 ppm$\Rightarrow \delta A_{\text{stat}} \sim 0.105$ ppm

High Resolution Spectrometers

Clean separation of elastic events by HRS optics



Locate detector over elastic line and integrate the flux



Large dispersion & heavy shielding reduce backgrounds at focal plane

Correcting Beam Asymmetries

$$A_{\text{raw}} = A_{\text{det}} - A_Q + \sum_{i=1,5} \beta_i \Delta x_i$$

- Slopes from
- natural beam jitter (regression)
 - **beam modulation** (dithering)

Independent methods provide a cross-check.
Each is subject to different systematic errors.

Regression:

- Natural beam motion, measure $dA/d\Delta x_i$
- Simultaneous fit establishes independent sensitivities
- By definition, removes correlation of asymmetry to beam *monitors*
- **Sensitive to highly correlated beam motion and electronics noise**

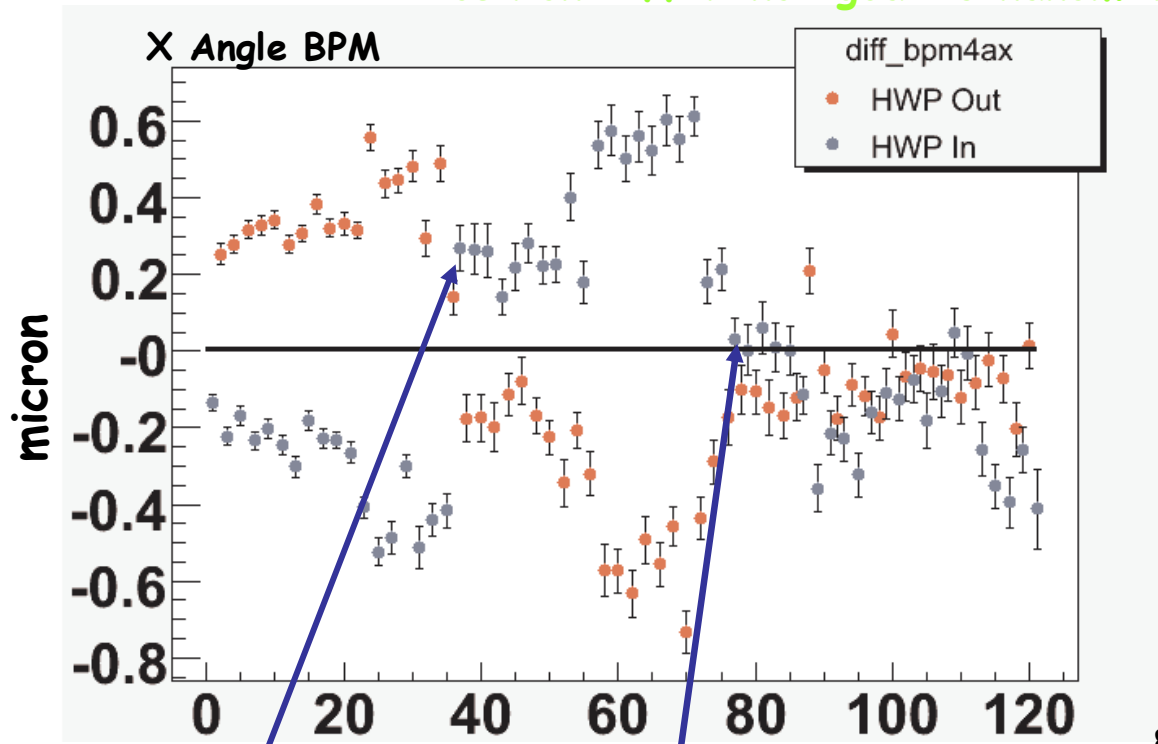
"Dithering":

- Induce non-HC beam motion with coils, measure dS/dC_i , dx_i/dC_i
- Relate slopes to dS/dx_i
- Not compromised by correlated beam motion
- **Robust, clear signals for failures**
- **Sensitive to non-linearities**

⇒ See Kent Paschke's talk

Beam Position Differences, Helium

Position difference goal: 3 nanometers!

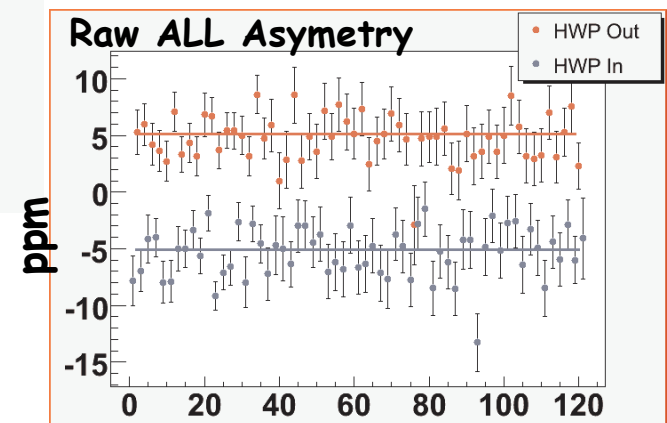


Helicity signal to driver reversed

Helicity signal to driver removed

All's well that ends well

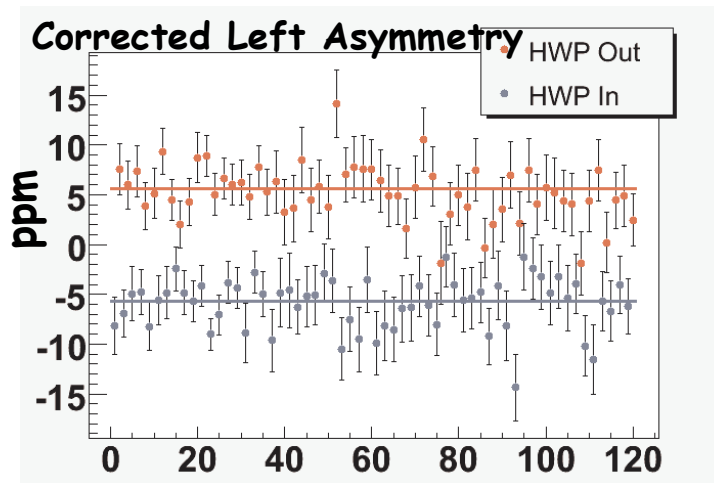
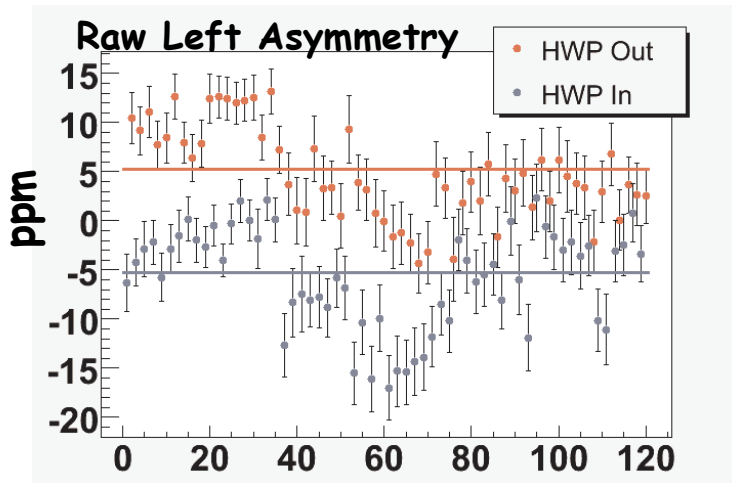
- Problem clearly identified as beam steering from electronic cross-talk
- No helicity-correlated electronics noise in Hall DAQ at $< \text{ppb}$ level
- Large position differences \approx cancel in average over both detectors



Problem: Helicity signal deflecting the beam through electronics "pickup"

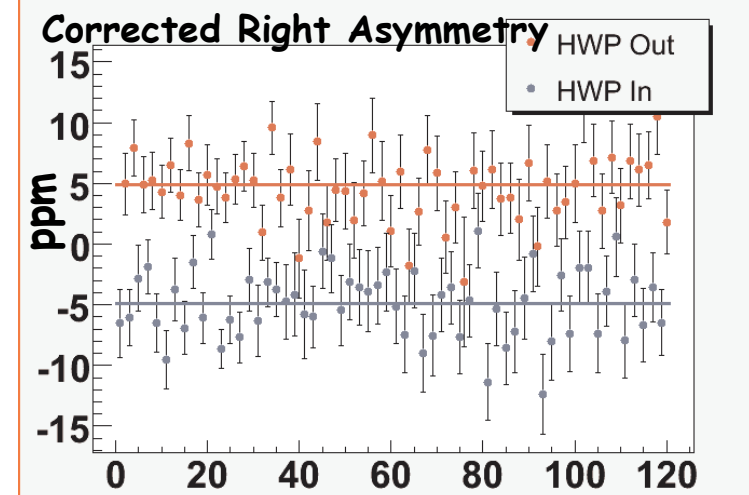
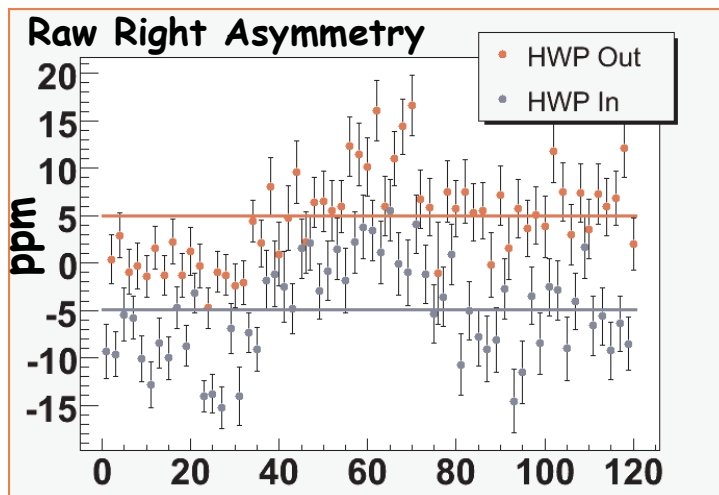
Large beam deflections even when Pockels cell is off

Beam Position Corrections, Helium



Beam Asymmetries

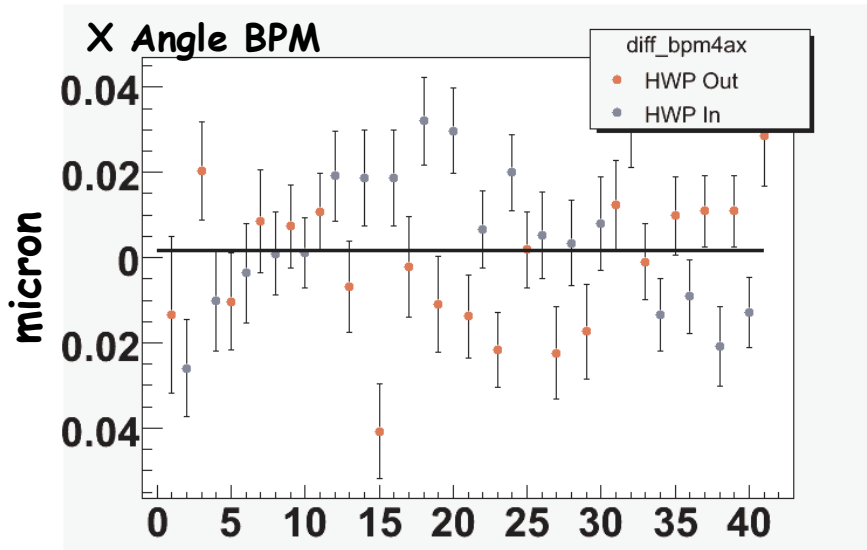
Energy: -3ppb
X Target: -5 nm
X Angle: -28 nm
Y Target: -21 nm
Y Angle: 1 nm



Total Corrections:

Left: -370 ppb
Right: 80 ppb
All: 120 ppb

Beam Position Corrections, Hydrogen



Surpassed Beam Asymmetry Goals
for Hydrogen Run

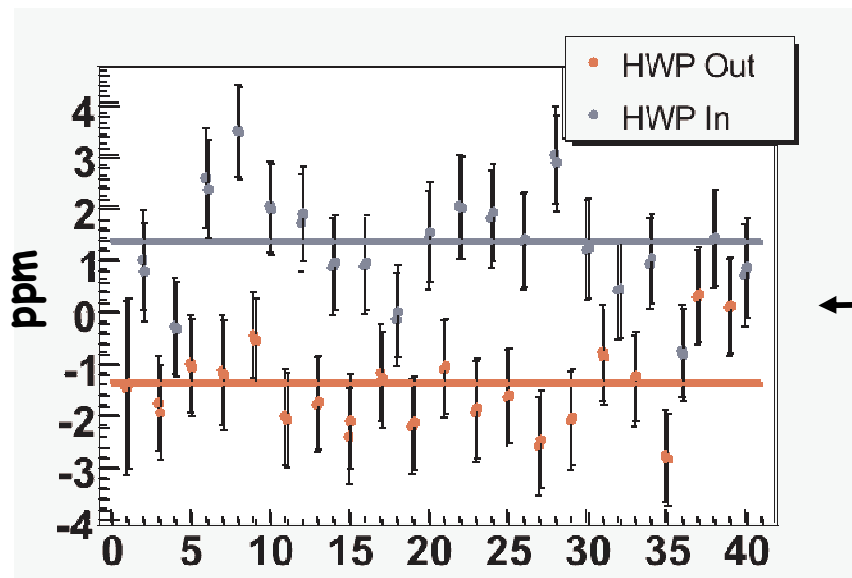
Energy: -0.25 ppb

X Target: 1 nm

X Angle: 2 nm

Y Target : 1 nm

Y Angle: <1 nm



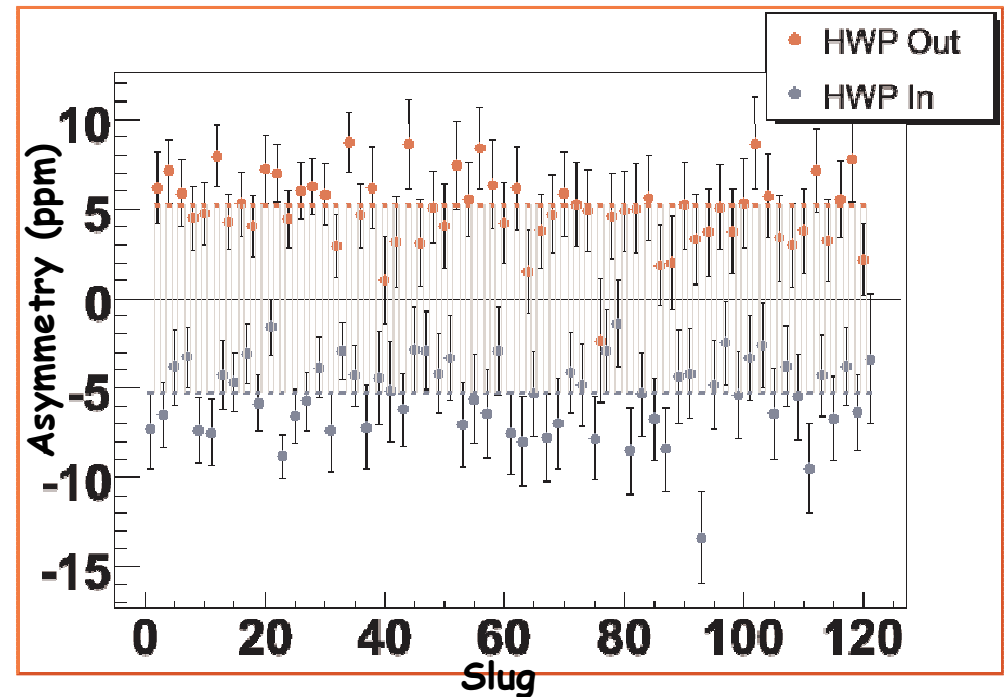
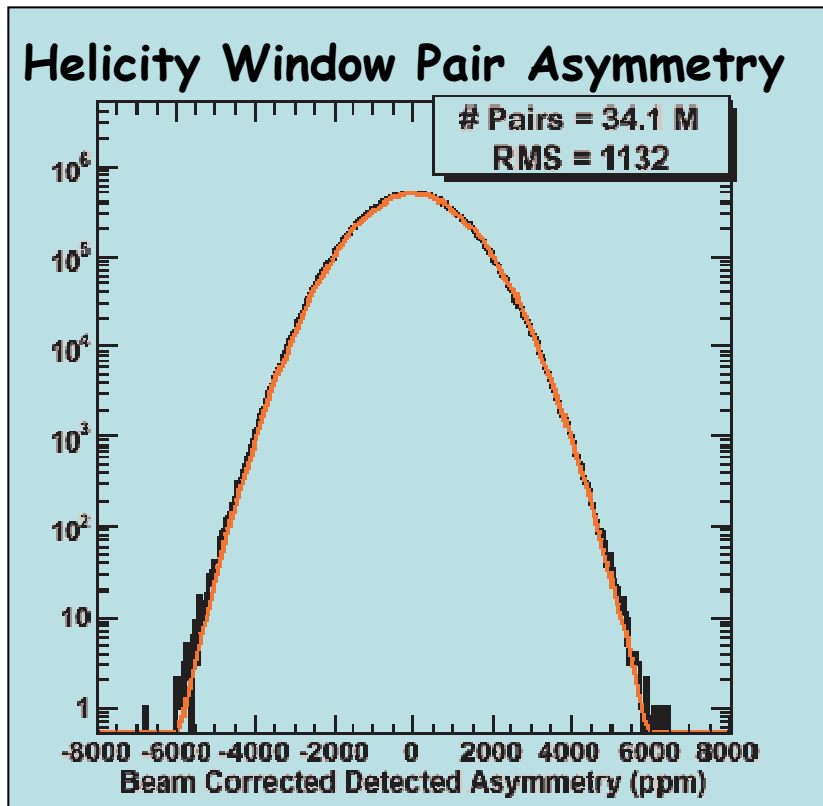
Corrected and Raw, Left arm alone,
Superimposed!

Total correction for beam position
asymmetry on Left, Right, or ALL
detector: **10 ppb**

^4He Preliminary Results

Raw Parity Violating Asymmetry

A_{raw} correction ~ 0.12 ppm



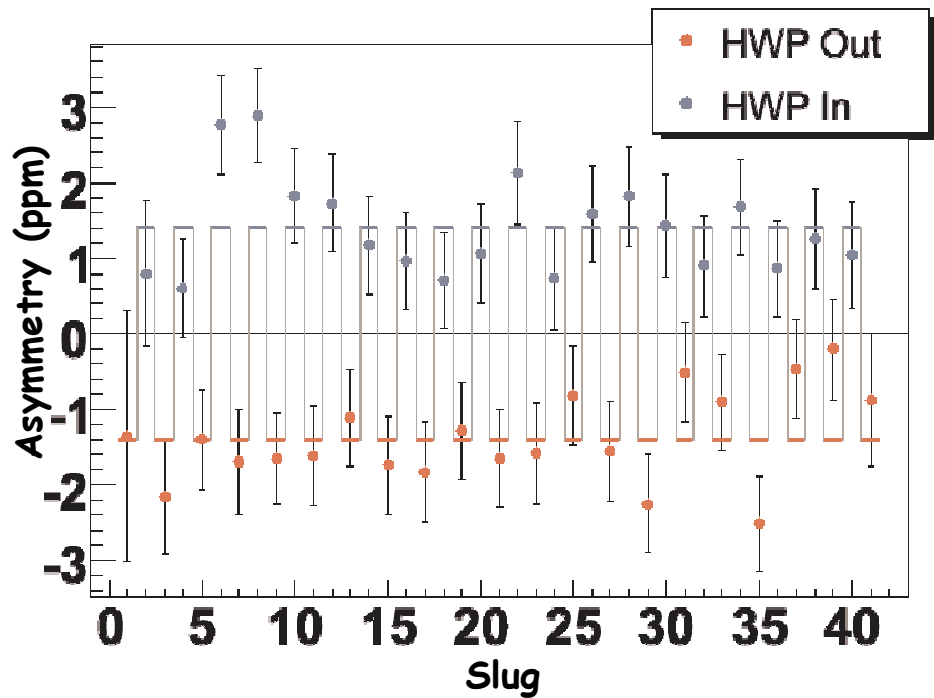
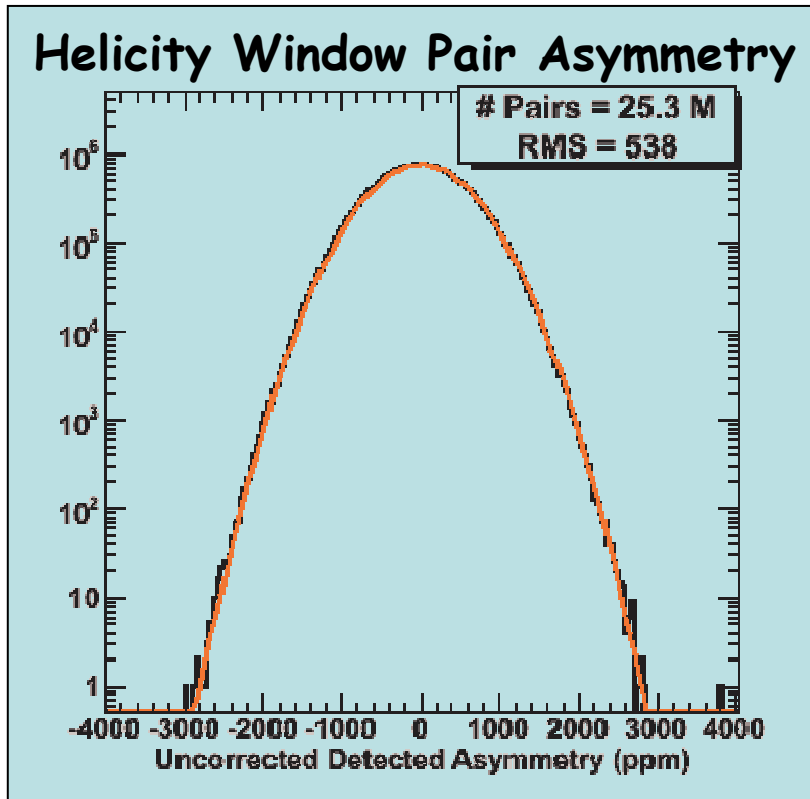
$$Q^2 = 0.07725 \pm 0.0007 \text{ GeV}^2$$

$$A_{\text{raw}} = 5.253 \text{ ppm} \pm 0.191 \text{ ppm (stat)}$$

^1H Preliminary Results

Raw Parity Violating Asymmetry

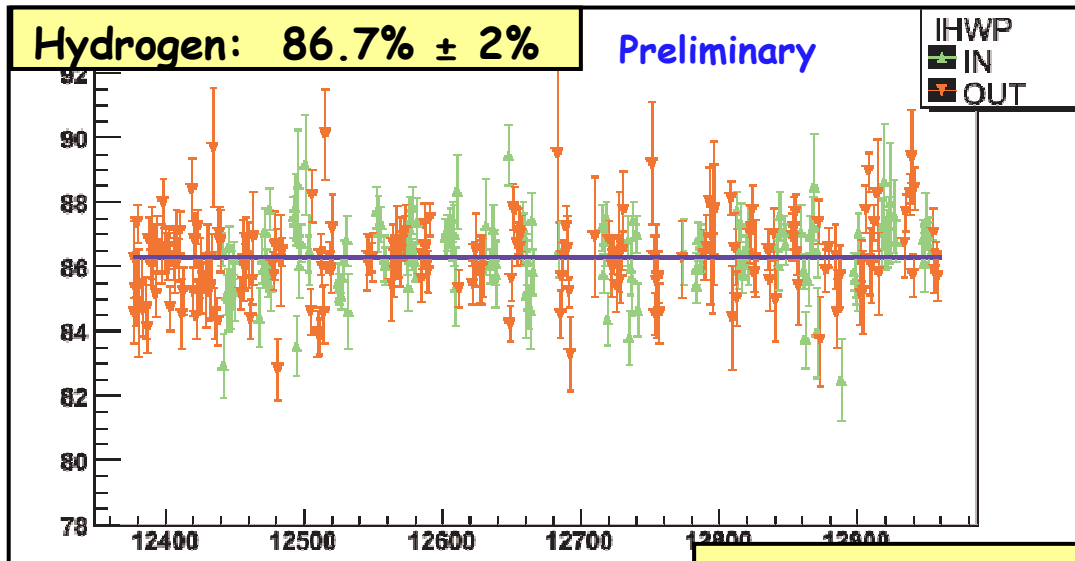
A_{raw} correction ~ 11 ppm



$$Q^2 = 0.1089 \pm 0.0011 \text{ GeV}^2$$

$$A_{\text{raw}} = -1.418 \text{ ppm} \pm 0.105 \text{ ppm (stat)}$$

Compton Polarimetry



Continuous, non-invasive

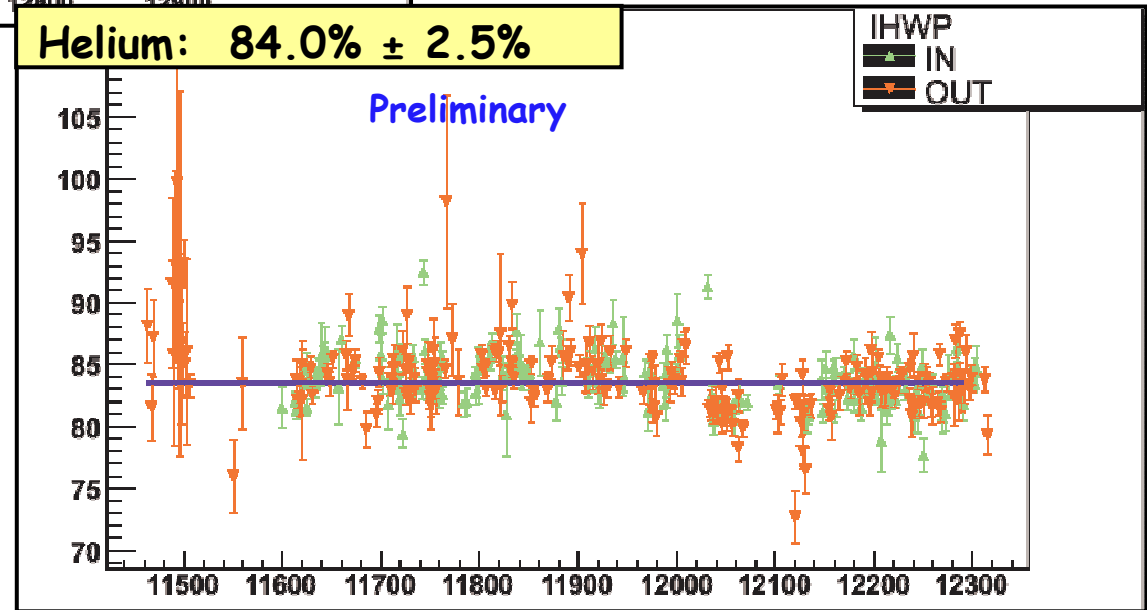
Here : Electron Detector analysis

Cross-checked with Møller, Mott
polarimeters

also: independent electron analysis

Helium ran with lower beam
energy, making the analysis
significantly more challenging.

New developments in both photon
and electron analyses in
preparation: anticipate $<2\%$
systematic uncertainty



Miscellany

- **Backgrounds:** ⇒ Bryan Moffit's talk

Dilutions:	2.2% (^4He)	0.8% (^1H)
Systematic	60 ppb (^4He)	16 ppb (^1H)
- **Q^2 & effective kinematics:** $\delta Q^2 < 1.0\%$ ⇒ Bryan Moffit's talk
- **Two-photon exchange corrections:**
small ⇒ Marc Vanderhaeghan's talk (no explicit correction made)
- **Transverse asymmetry:**
measured directly in dedicated runs, \approx cancels in left-right sum;
Systematic: 4 ppb (^1H) 8 ppb (^4He) ⇒ Lisa Kaufmann's talk
- **Electromagnetic Form Factors:** use Friedrich & Walcher parameterization, Eur. Phys. J. A, 17, 607 (2003), and BLAST data for G_E^n
- **Axial Form Factor:** highly suppressed for ^1H (not present for ^4He)
- **Vector Electroweak Radiative Corrections:** Particle Data Group
- **Blinded Analysis**

${}^4\text{He}$: Nuclear Effects

$0^+ \rightarrow 0^+ \quad T=0$ transition

- Any one-body electroweak operator O : (eg Fetter and Walecka)

$$\langle J,T | O | J,T \rangle = \sum \psi_{J,T}(\alpha, \alpha') \langle \alpha' | O | \alpha \rangle$$

one-body density matrix element
(nuclear structure)

single-particle matrix element
(nucleon structure)

 $|\alpha\rangle =$ complete set
- Asymmetry involves ratio of weak/EM matrix elements (G_E^S and $G_E^{T=0}$):
 Single term in J, T in transition; O same in weak and EM except for couplings
 → same one-body density matrix elements in numerator/denominator
 → nuclear structure cancels, only nucleon form factors remain

This result is **EXACT**, *if* :

- ${}^4\text{He}$ g.s. pure isospin state: Ramavataram, Hadjimichael, Donnelly PRC 50(1994)1174
 - No D-state admixture: Musolf & Donnelly PL B318(1993)263
 - Meson exchange corrections small: Musolf, Schiavilla, Donnelly PRC 50(1994)2173
- Nuclear effects all $\ll 1\%$, no explicit correction made.

HAPPEX

Error Budget-Helium

2005

False Asymmetries	48 ppb
Polarization	192 ppb
Linearity	58 ppb
Radiative Corrections	6 ppb
Q ² Uncertainty	58 ppb
Al background	32 ppb
Helium quasi-elastic background	24 ppb
Total	216 ppb

2004

False Asymmetries	103 ppb
Polarization	115 ppb
Linearity	78 ppb
Radiative Corrections	7 ppb
Q ² Uncertainty	66 ppb
Al background	14 ppb
Helium quasi-elastic background	86 ppb
Total	205 ppb

Error Budget-Hydrogen

2005

False Asymmetries	17 ppb
Polarization	37 ppb
Linearity	15 ppb
Radiative Corrections	3 ppb
Q ² Uncertainty	16 ppb
Al background	15 ppb
Rescattering Background	4 ppb
Total	49 ppb

2004

False Asymmetries	43 ppb
Polarization	23 ppb
Linearity	15 ppb
Radiative Corrections	7 ppb
Q ² Uncertainty	12 ppb
Al background	16 ppb
Rescattering Background	32 ppb
Total	63 ppb

HAPPEX-II 2005 Preliminary Results

HAPPEX-⁴He:

$$Q^2 = 0.0772 \pm 0.0007 \text{ (GeV/c)}^2$$
$$A_{PV} = +6.43 \pm 0.23 \text{ (stat)} \pm 0.22 \text{ (syst) ppm}$$

$$A(G^s=0) = +6.37 \text{ ppm}$$

$$G^s_E = 0.004 \pm 0.014_{\text{(stat)}} \pm 0.013_{\text{(syst)}}$$

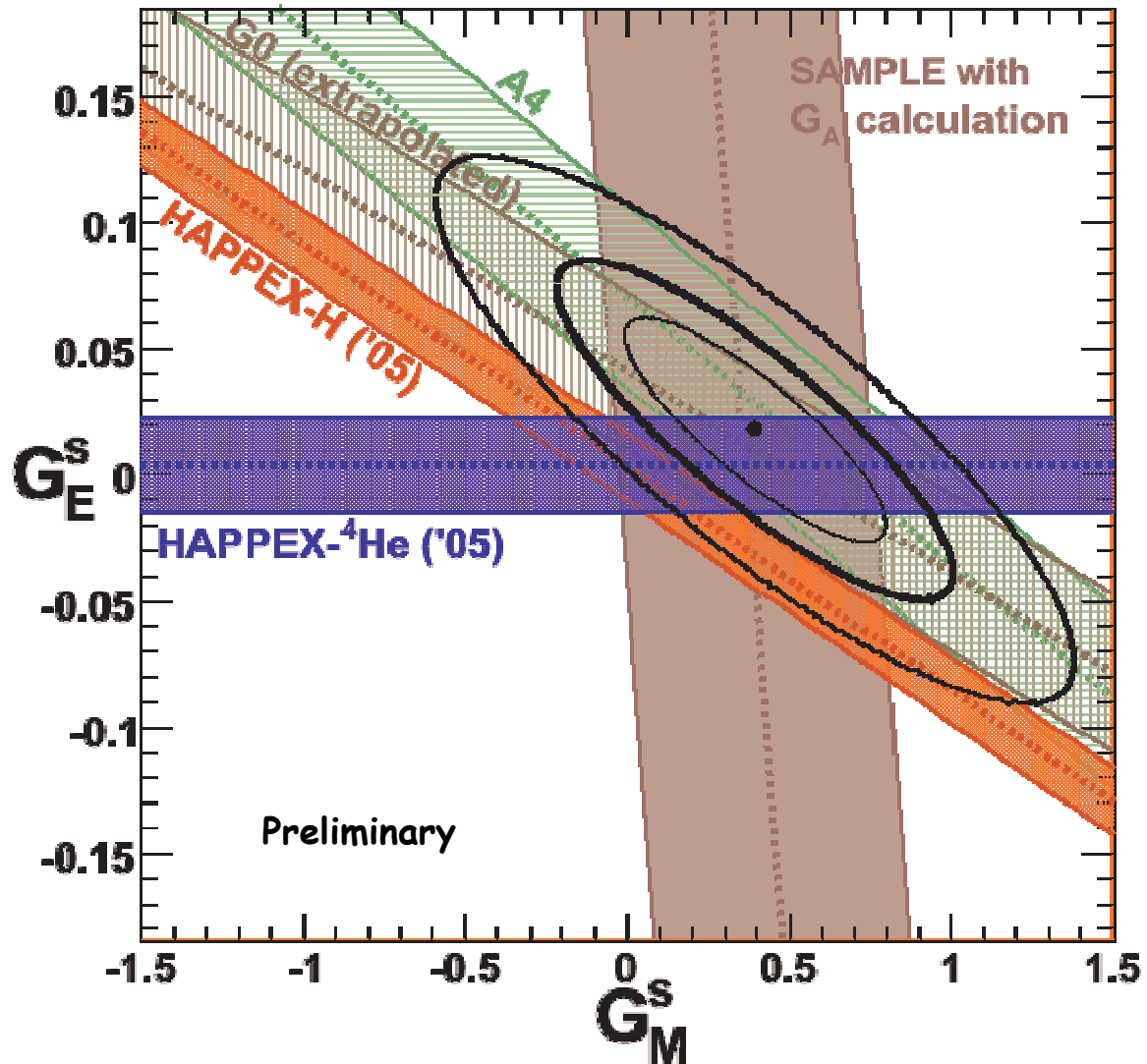
HAPPEX-H:

$$Q^2 = 0.1089 \pm 0.0011 \text{ (GeV/c)}^2$$
$$A_{PV} = -1.60 \pm 0.12 \text{ (stat)} \pm 0.05 \text{ (syst) ppm}$$

$$A(G^s=0) = -1.640 \text{ ppm} \pm 0.041 \text{ ppm}$$

$$G^s_E + 0.088 G^s_M = 0.004 \pm 0.011_{\text{(stat)}} \pm 0.005_{\text{(syst)}} \pm 0.004_{\text{(FF)}}$$

HAPPEX-II 2005 Preliminary Results

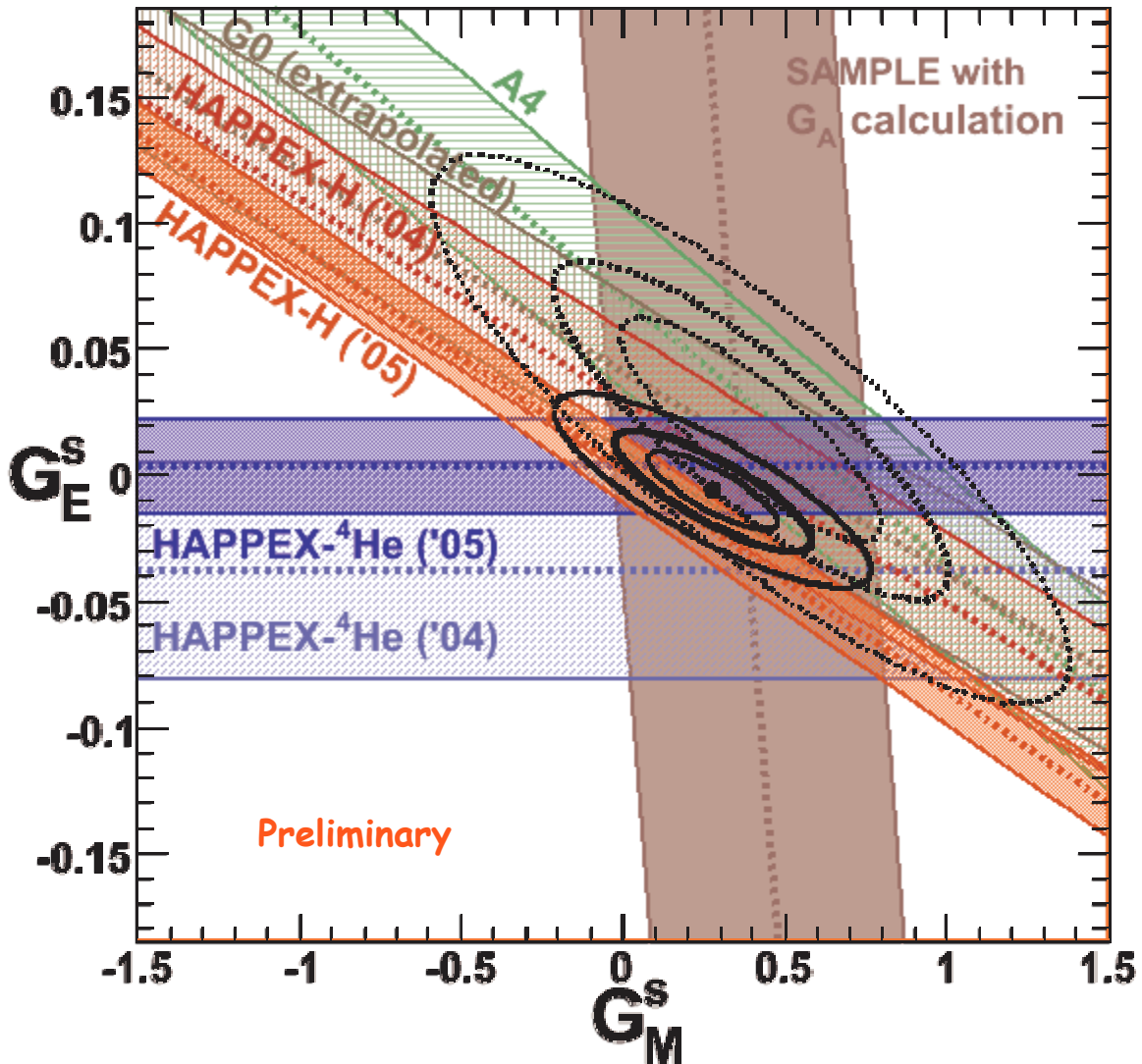


Three bands:

1. Inner: Project to axis for 1-D error bar
2. Middle: 68% probability contour
3. Outer: 95% probability contour

Caution: the combined fit is approximate. Correlated errors and assumptions not taken into account

World Data near $Q^2 \sim 0.1 \text{ GeV}^2$



$$G_M^s = 0.28 \pm 0.20$$

$$G_E^s = -0.006 \pm 0.016$$

$\sim 3\% \pm 2.3\%$ of proton magnetic moment

$\sim 0.2 \pm 0.5\%$ of electric distribution

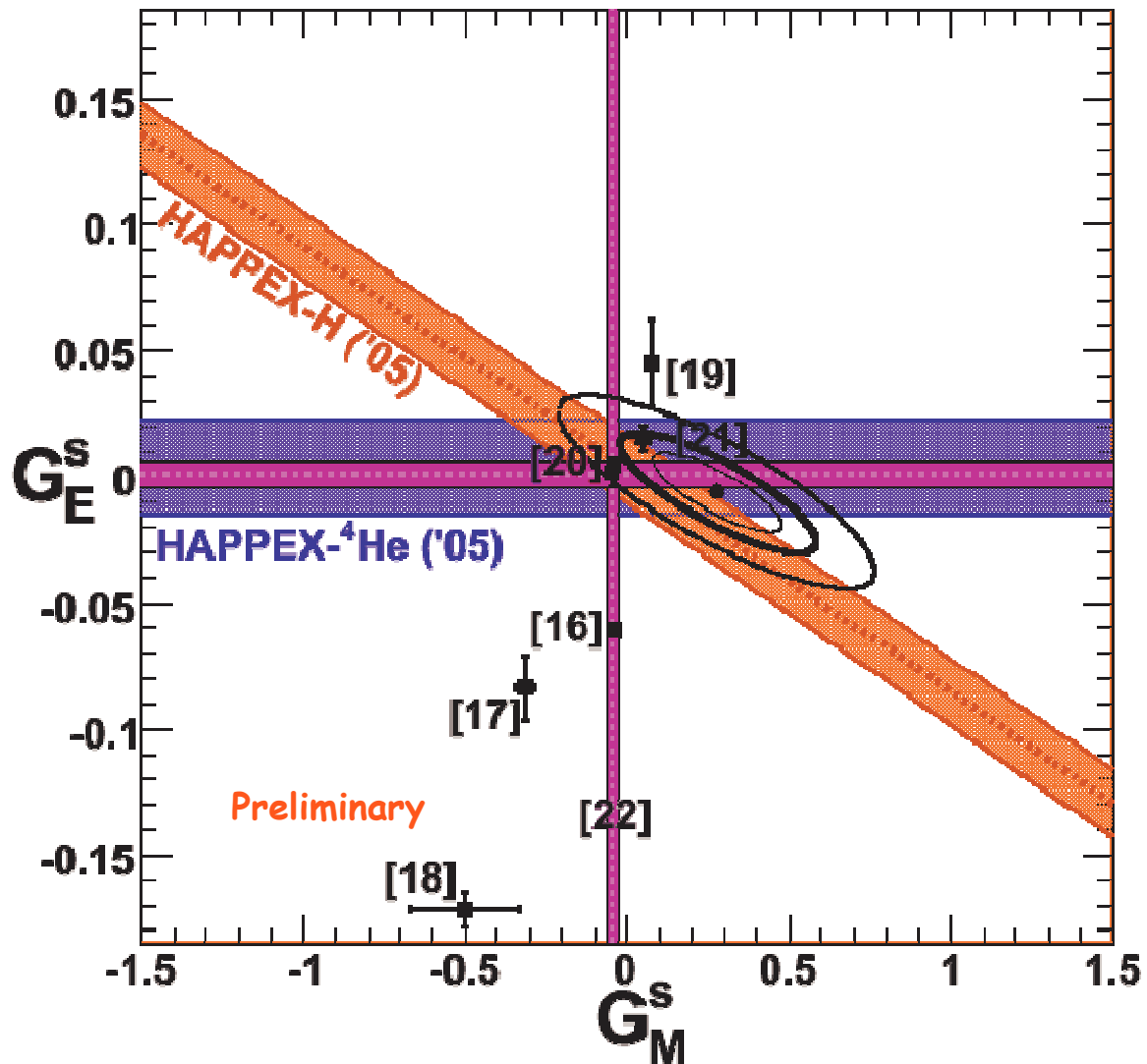
HAPPEX-only fit suggests something even smaller:

$$G_M^s = 0.12 \pm 0.24$$

$$G_E^s = -0.002 \pm 0.017$$

Caution: the combined fit is approximate. Correlated errors and assumptions not taken into account

World data consistent with state of the art theoretical predictions



16. **Skyrme Model** - N.W. Park and H. Weigel, Nucl. Phys. A **451**, 453 (1992).
17. **Dispersion Relation** - H.W. Hammer, U.G. Meissner, D. Drechsel, Phys. Lett. B **367**, 323 (1996).
18. **Dispersion Relation** - H.-W. Hammer and Ramsey-Musolf, Phys. Rev. C **60**, 045204 (1999).
19. **Chiral Quark Soliton Model** - A. Sliva *et al.*, Phys. Rev. D **65**, 014015 (2001).
20. **Perturbative Chiral Quark Model** - V. Lyubovitskij *et al.*, Phys. Rev. C **66**, 055204 (2002).
21. **Lattice** - R. Lewis *et al.*, Phys. Rev. D **67**, 013003 (2003).
22. **Lattice + charge symmetry** - Leinweber *et al.*, Phys. Rev. Lett. **94**, 212001 (2005) & hep-lat/0601025



See Ross Young's talk

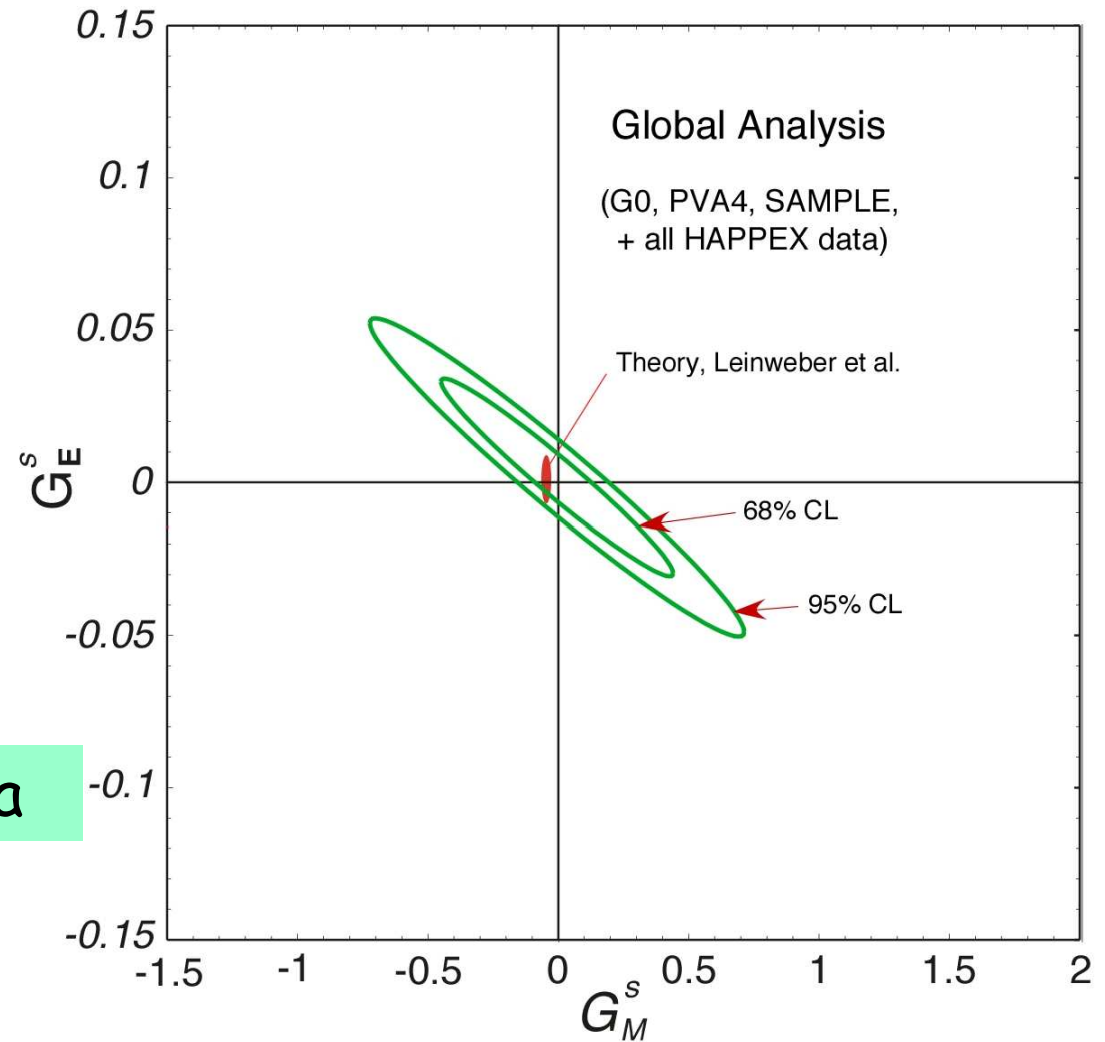
A Global Fit: R.D. Young, et al. nucl-ex/0604010

- all data $Q^2 < 0.3$, leading moments of G_E^s , G_M^s

- Kelly's EMF

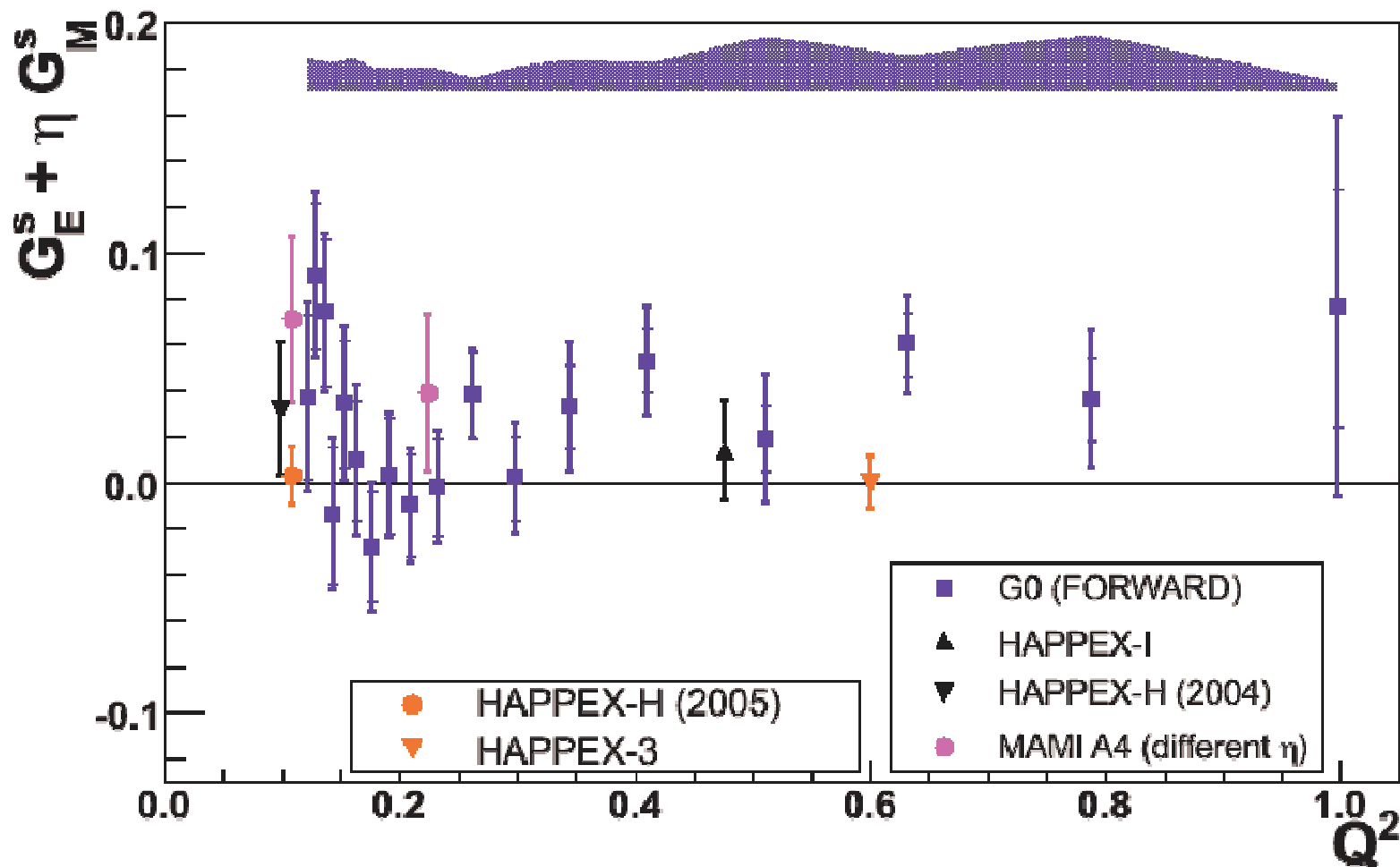
- Float G_A^e separately
for neutron and proton

With HAPPEX-2005 data



Figures: courtesy of R. Carlini, R. Young

Future: HAPPEX-3 (2008)



Conclusions

- *Marvelous* consistency of data.
- $Q^2 = 0.1 \text{ GeV}^2$: G_M^s and G_E^s consistent with zero; constraining axial FF to Zhu *et al.* theory favors positive G_M^s
 - ^4He : best fractional error in PV experiment to date ($< 4\%$)
no axial contamination \rightarrow uniquely determines G_E^s
 - ^1H : < 100 ppb error on A , unprecedented "parity quality"
- Still room (& hints?) for non-zero values at higher Q^2

Future of Strangeness form factors:

- GO Backward: will allow G_M^s and G_E^s separation at two Q^2
- Mainz: PV-A4 backward-angle program well underway
- HAPPEX-III: high precision forward-angle @ $Q^2 = 0.6 \text{ GeV}^2$