

Pointing Update

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Pointing

- Determine the center scattering angle
- Elastic scattering off a target of mass M

$$E' = \frac{E - E_{loss}}{1 + \frac{2(E - E_{loss}) \sin^2(\theta / 2)}{M}} - E'_{loss}$$

- Use the difference in E' between two nuclei

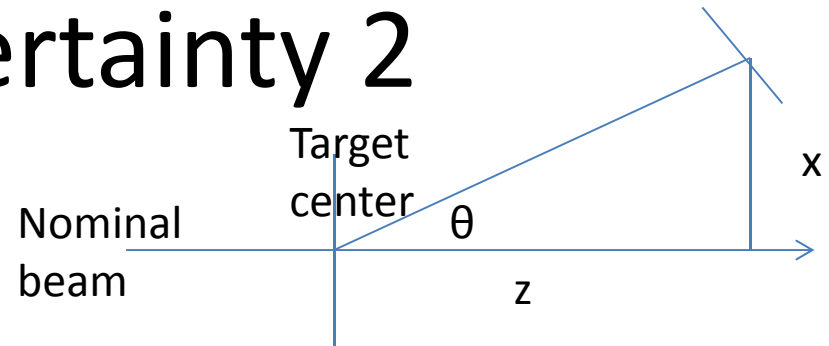
$$\Delta E' = E'_1 - E'_2 = \frac{E}{1 + \frac{2E \sin^2(\theta_1 / 2)}{M_1}} - \frac{E}{1 + \frac{2E \sin^2(\theta_2 / 2)}{M_2}} - (E'_{1loss} - E'_{2loss})$$

If two nuclei are in the same target, like CH₂, $\theta_1 = \theta_2 = \theta$, E_{loss} cancels each other

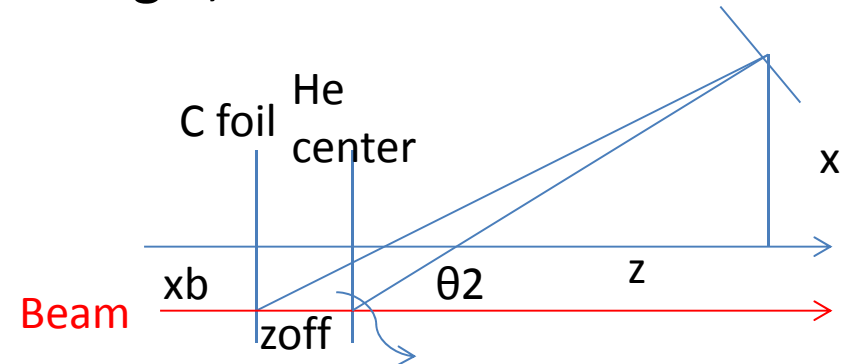
If not, like C in LHe, more steps need to be considered

Pointing Uncertainty 2

- Survey
- $\theta = \text{atan}(x/z)$
- If just use survey to determine the angle, $\delta\theta \sim 0.7mr$



- $\theta_1 = \text{atan}((x - x_b)/z)$
- $\theta_2 = \text{atan}((x - x_b)/(z + z_{\text{off}}))$



$$\Delta E' = E'_1 - E'_2 = \frac{E}{1 + \frac{2E \sin^2(\theta_1/2)}{M_1}} - \frac{E}{1 + \frac{2E \sin^2(\theta_2/2)}{M_2}} - (E'_{1\text{loss}} - E'_{2\text{loss}})$$

- $\theta_1 = \theta + (\theta_1 - \theta)$ vs. $\theta_1 = \theta * (\theta_1/\theta)$
- Do similar substitution for θ_2

Obtained from $x, x_b, z, z_{\text{off}}$

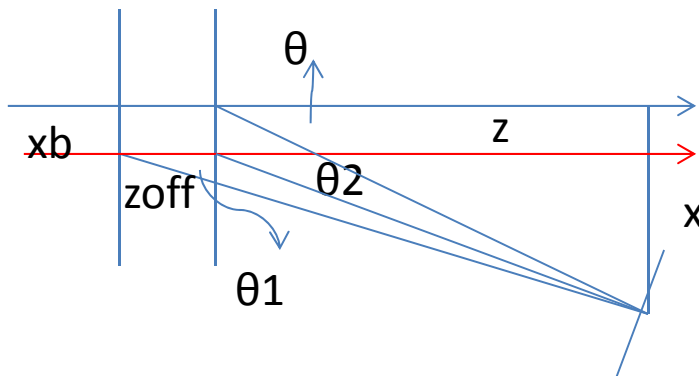
Pointing Uncertainty 2

- Survey uncertainty $\delta x = 0.5\text{mm}$
- Beam_x uncertainty $\delta x_b = 1.5\text{mm}$
- Target position uncertainty $\delta z = 1.8\text{mm}$
- C relative position $\delta z_{\text{off}} = 0.15\text{mm}$
- θ_1/θ , uncertainty $\sim 0.2\text{mr}$
- $\theta_1 - \theta$, uncertainty $\sim 0.04\text{mr}$!

Results

	Pointing values (rad)	Survey values (rad)
LHRS	0.0997 +/- 0.0002	0.1007 +/- 0.0008
RHRS	0.1073 +/- 0.0005	0.1009 +/- 0.0008

$$\frac{\Delta E' = E'_1 - E'_2}{0.0046 \text{ GeV}} = \frac{E}{1 + \frac{2E \sin^2(\theta_1 / 2)}{M_1}} - \frac{E}{1 + \frac{2E \sin^2(\theta_2 / 2)}{M_2}} - \frac{(E'_{1loss} - E'_{2loss})}{0.247/1000 \text{ GeV}}$$



Doing & todo

- Summary for the pointing study so far
- CH2 run in the longitudinal setting to cross check

Backup

Pointing Uncertainty

- Uncertainty calculation – $\theta \sim 6^\circ$, $E = 2.254 \text{ GeV}$
 - Two nuclei in the same target

$$\sin \theta d\theta = -4.9 \times 10^{-3} dE + 1.11 d(\Delta E')$$

- Use C12 ground state and 1st excited state to calibrate $d(\Delta E')$
 - Nominal value is 4.44 MeV
 - LHRS 4.42 MeV, RHRS 4.39 MeV
- $d\theta \sim 0.2 \text{ mr (L), } 0.5 \text{ mr (R)}$
- $d\theta/\theta < 1\%$

