

E12-07-108 (GMp)

Precision Measurement of the Proton Elastic Cross Section at High Q^2

PAC32 12 GeV Proposal : PR12-07-108

Spokespersons: Bryan Moffit (MIT)
Shalev Gilad (MIT)
Bogdan Wojtsekhowski (JLab)
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Grading and beam time were considered by PAC35:

PR12-07-108: The PAC recommends a beam time assignment of 24 days, compared with the request for 31 days, by asking the experimentalists not to pursue a measurement at the highest Q^2 point.

SLAC first measurement

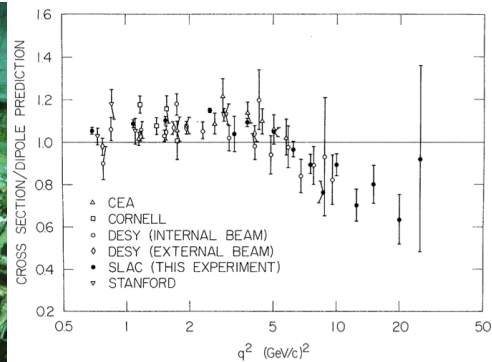
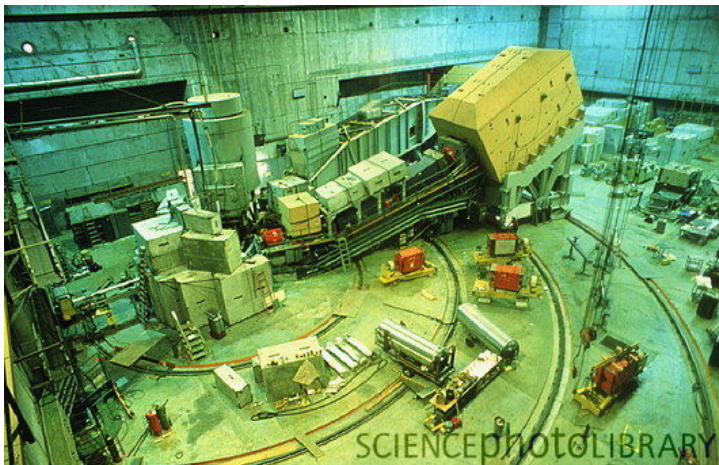


FIG. 1. Compilation of electron-proton elastic-scattering cross sections for q^2 greater than $0.7 (\text{GeV}/c)^2$. The cross sections are normalized to the Rosenbluth formula and the dipole relation. Systematic errors in the SLAC data are not shown, but would be up to 6%.

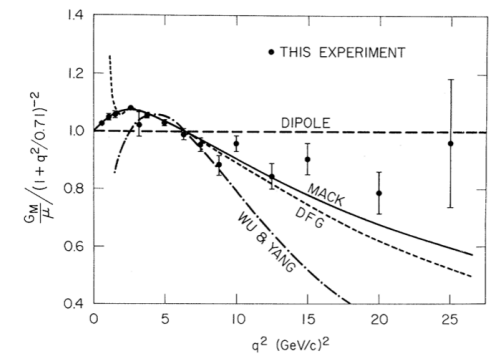


FIG. 2. Comparison of several theoretical expressions for G_M/μ and the SLAC data from Table I. Details of the fits are given in the text.

SLAC results in 1968

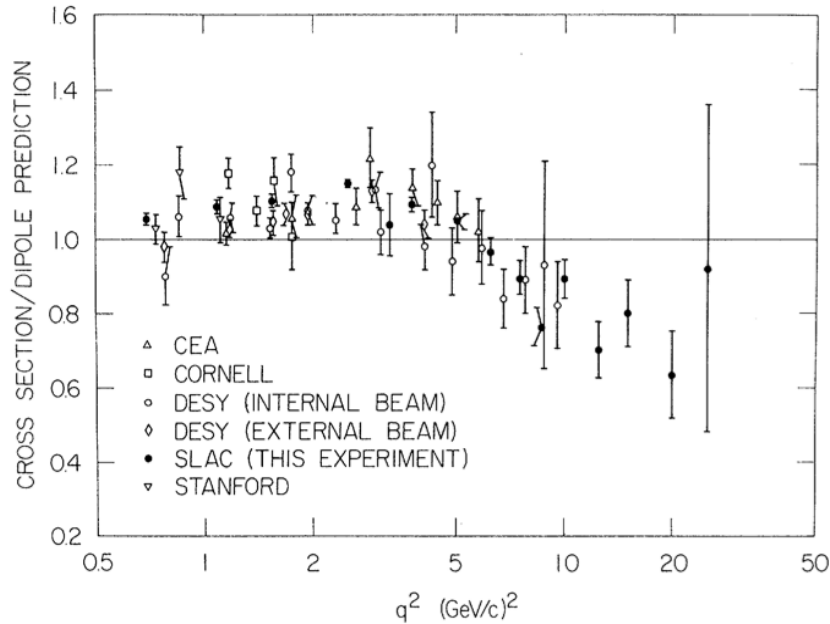


FIG. 1. Compilation of electron-proton elastic-scattering cross sections for q^2 greater than $0.7 (\text{GeV}/c)^2$. The cross sections are normalized to the Rosenbluth formula and the dipole relation. Systematic errors in the SLAC data are not shown, but would be up to 6%.

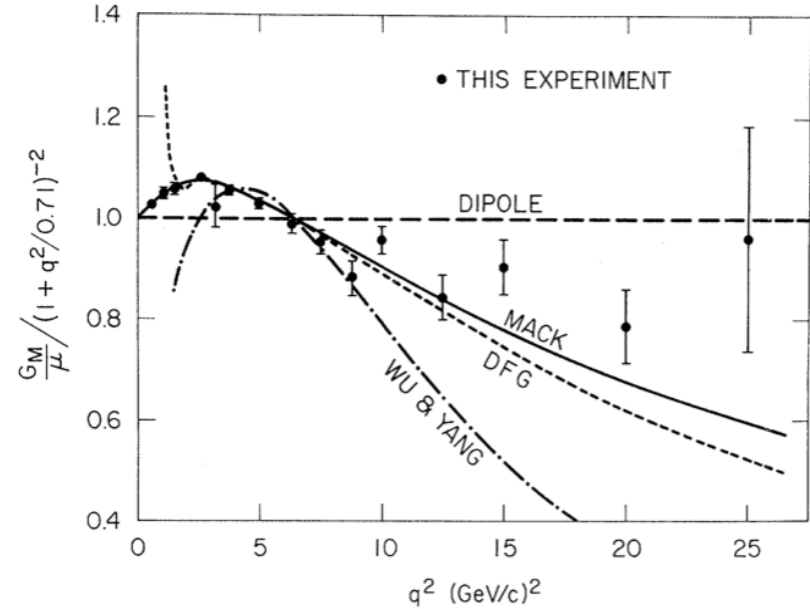


FIG. 2. Comparison of several theoretical expressions for G_M/μ and the SLAC data from Table I. Details of the fits are given in the text.

PRL 20, 292 (1968), G_M scales to $G_D = 1/(1+Q^2/0.71)^2$

SLAC results for the proton Form Factors

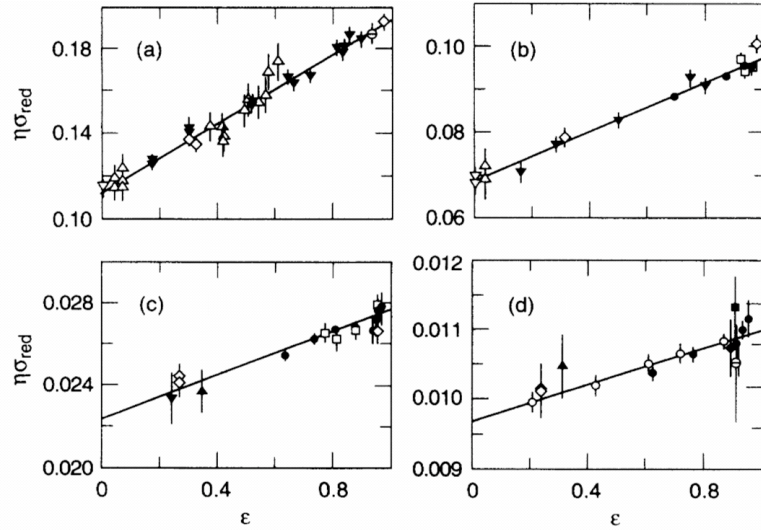
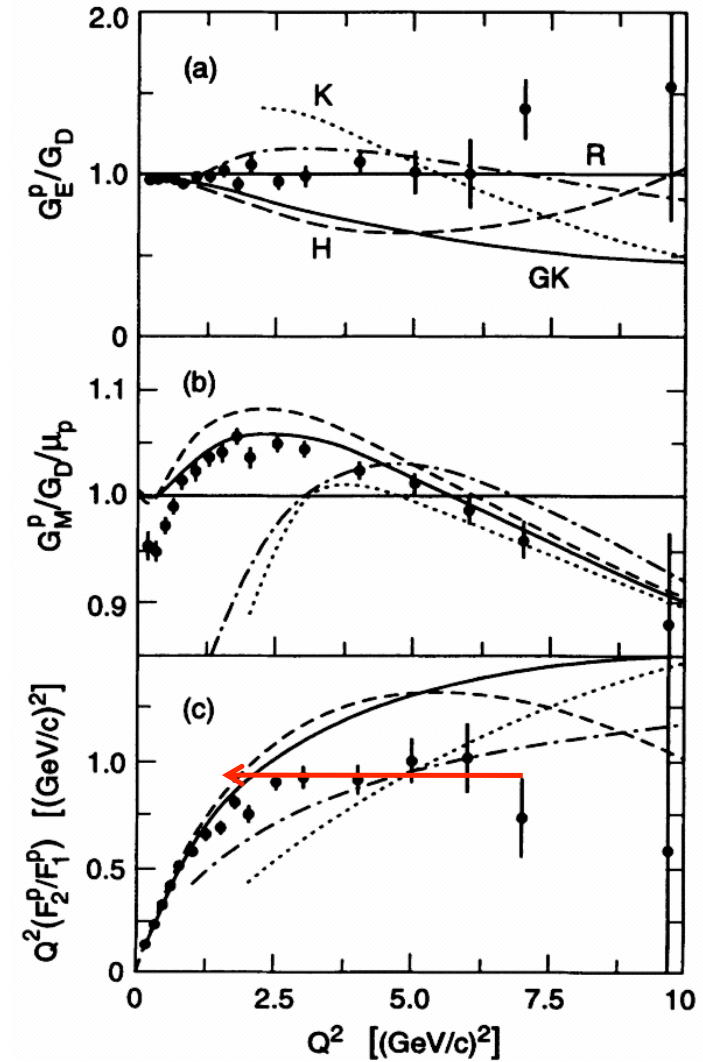
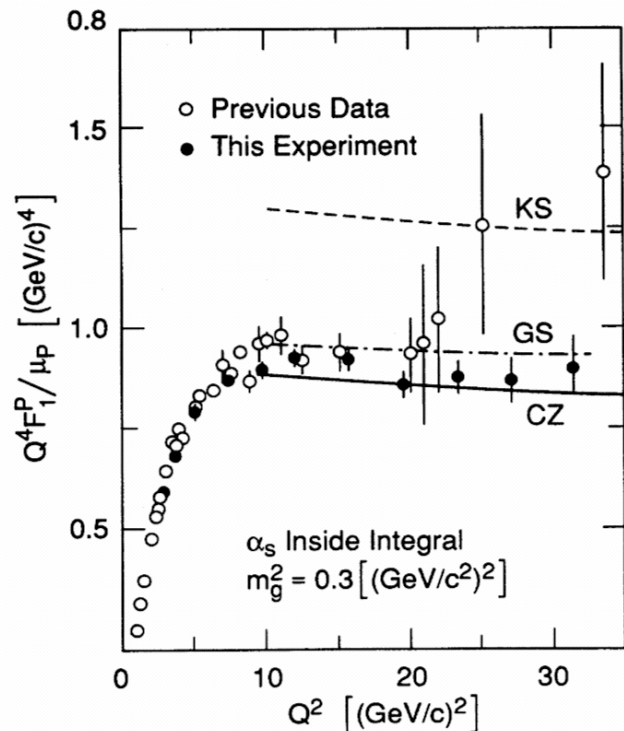


FIG. 9. Four typical Rosenbluth fits for the form factor extraction from the global data set at (a) $Q^2 = 0.6$, (b) $Q^2 = 1.0$, (c) $Q^2 = 2.0$, and (d) $Q^2 = 3.0$ (GeV/c)².

Walker et al
(1993)

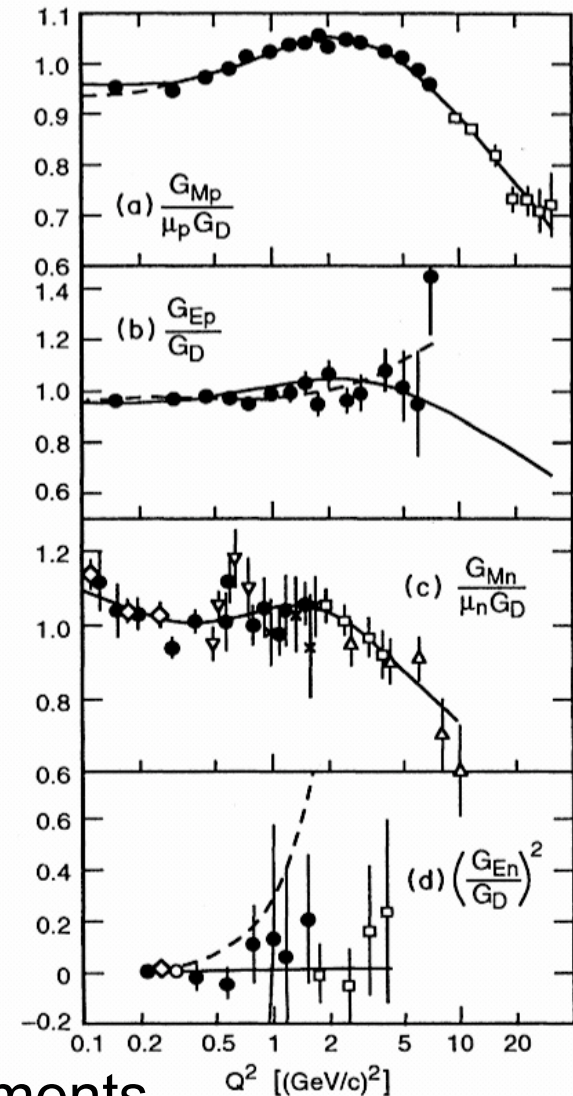


SLAC results for the Form Factors



Sill et al
(1993)

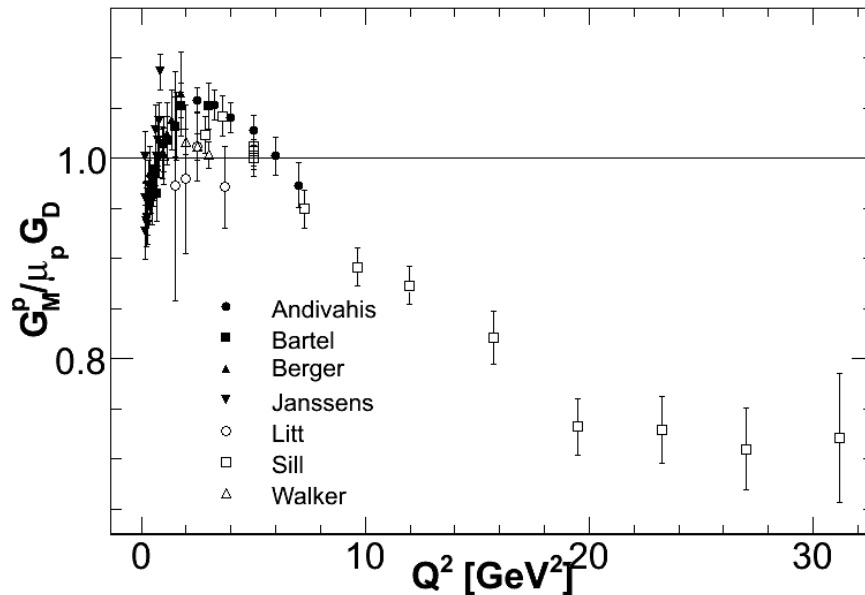
Bosted
(1995)



What does it mean?

These are the (e,e') single arm measurements

Form Factors - High Q^2



Predictions from QCD?

QCD Lagrangian:

- Nucleon Structure in terms of quark and gluon degrees of freedom

GPDs:

- How does the active quark couple to the proton?

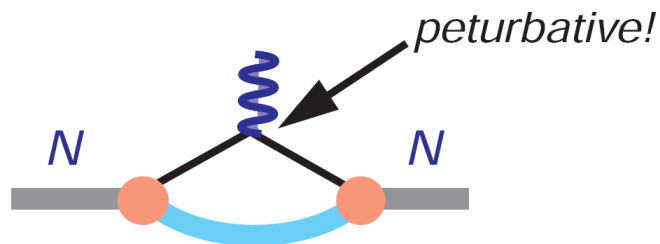


Figure from 12 GeV Upgrade pCDR

$$F_1(t) = \int_{-1}^{+1} \sum_q dx H^q(x, \xi, t) dx$$

$$F_2(t) = \int_{-1}^{+1} \sum_q dx E^q(x, \xi, t) dx$$



Form Factor Scaling

At high values of Q^2 ,
asymptotic freedom [small $\alpha_s(Q^2)$] allows for pQCD calculations.

How high is that?

Dimensional Scaling:
Form Factors scale
asymptotically as $(Q^2)^{-(n-1)}$
 n = participating valence quarks

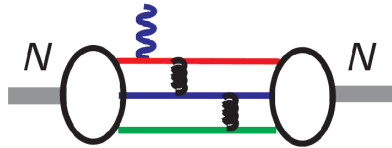
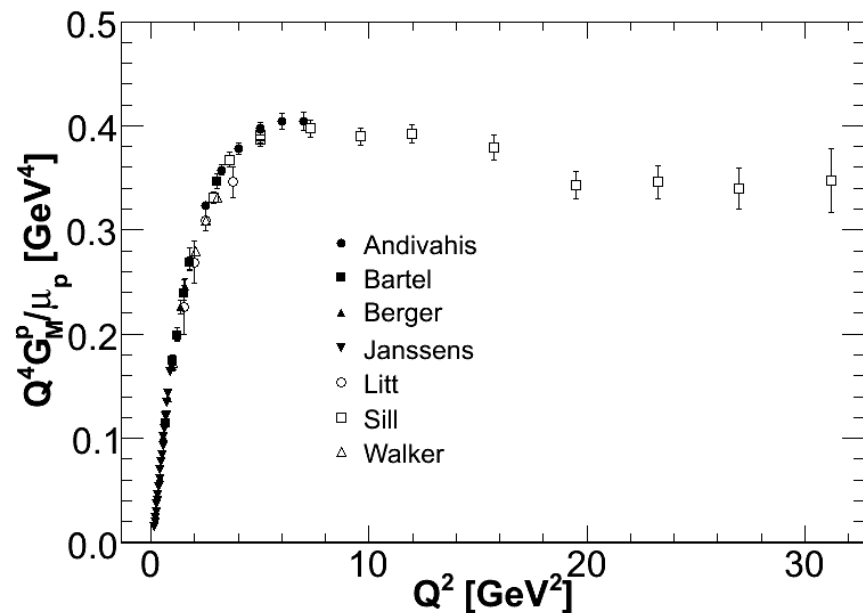


Figure from 12 GeV Upgrade pCDR

$$Q^4 G_M^p \propto Q^4 F_1^p \sim \text{constant}$$

pQCD $\rightarrow$ logarithmic departures from Q^2 dependence



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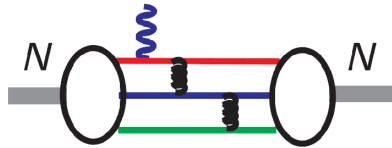
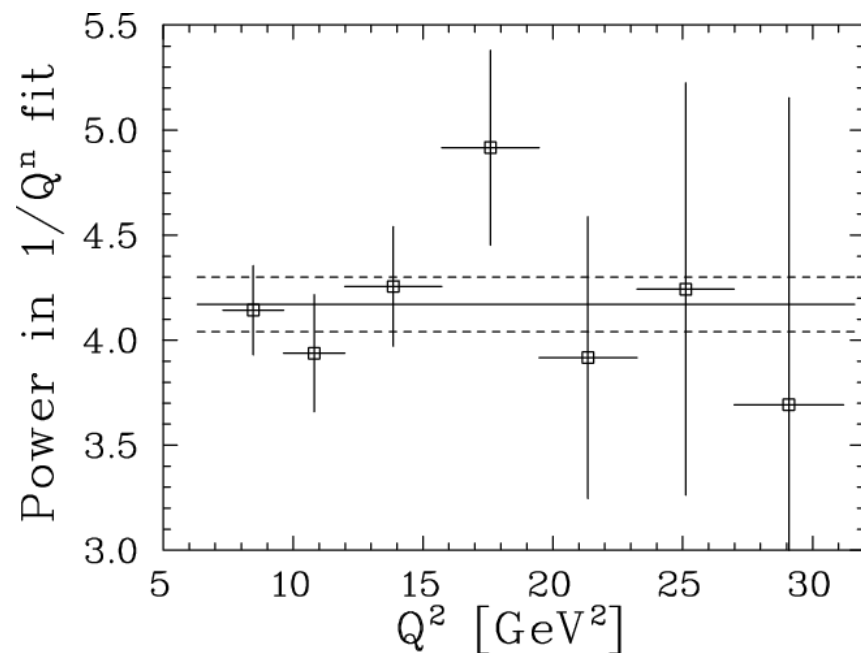


Figure from 12 GeV Upgrade pCDR

$$Q^4 G_M^p \propto Q^4 F_1^p \sim \text{constant}$$

pQCD $\rightarrow$ logarithmic departures from Q^2 dependence



Cross Section $\rightarrow$ Form Factors

$$\frac{d\sigma}{d\Omega} = \sigma_{Mott} \frac{\epsilon (G_E^p)^2 + \tau (G_M^p)^2}{\epsilon (1 + \tau)}$$

$$\tau = \frac{Q^2}{4M_p^2}$$

$$\epsilon = [1 + 2(1 + \tau) \tan^2(\theta/2)]^{-1}$$

Rosenbluth Separation

- Measure Cross Section at same Q^2 but different E and θ (varying ϵ)
- At sufficiently high Q^2 , G_M^p dominates.

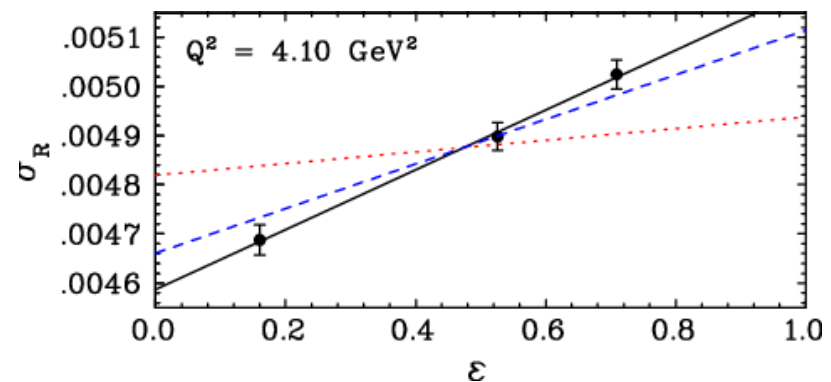


Figure from Qattan et al. PRL 94 (2005) 142301



Cross Section -> Form Factors

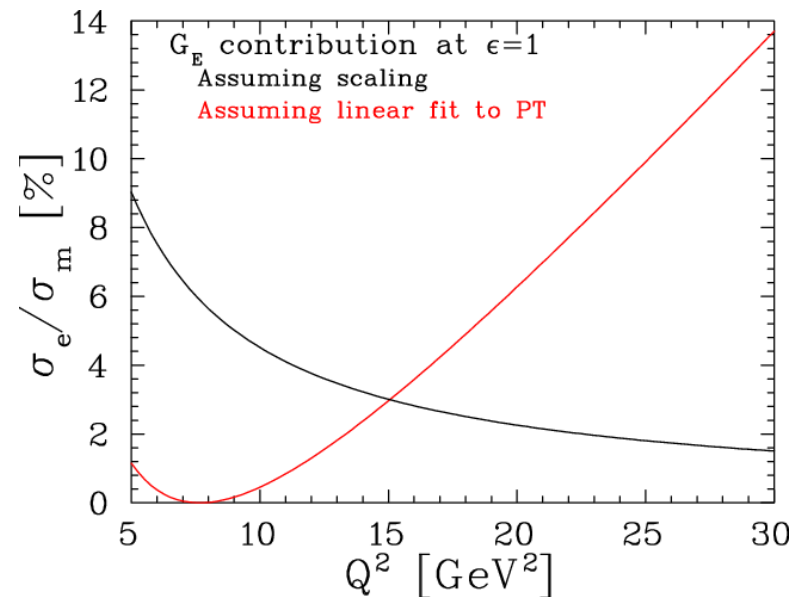
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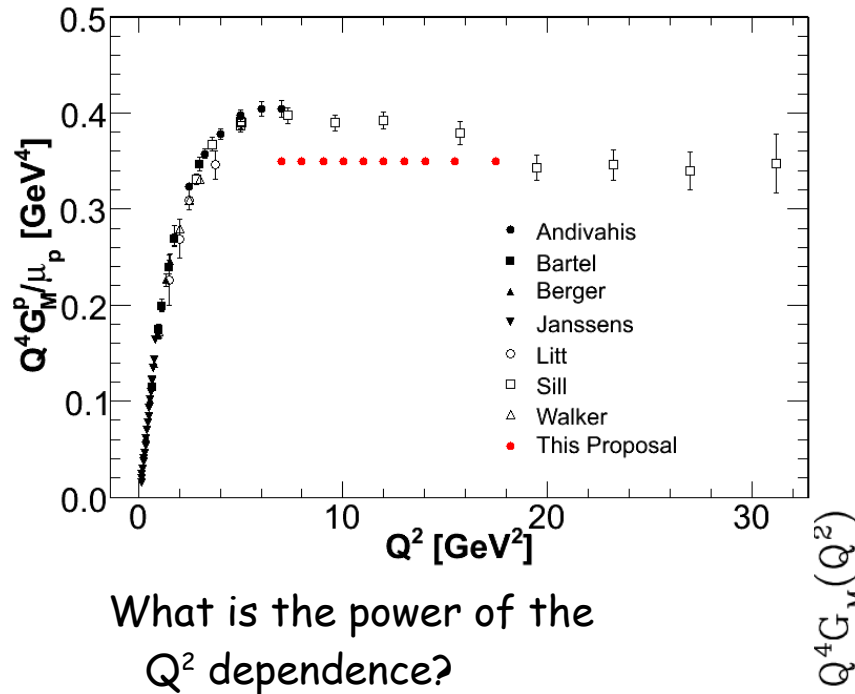
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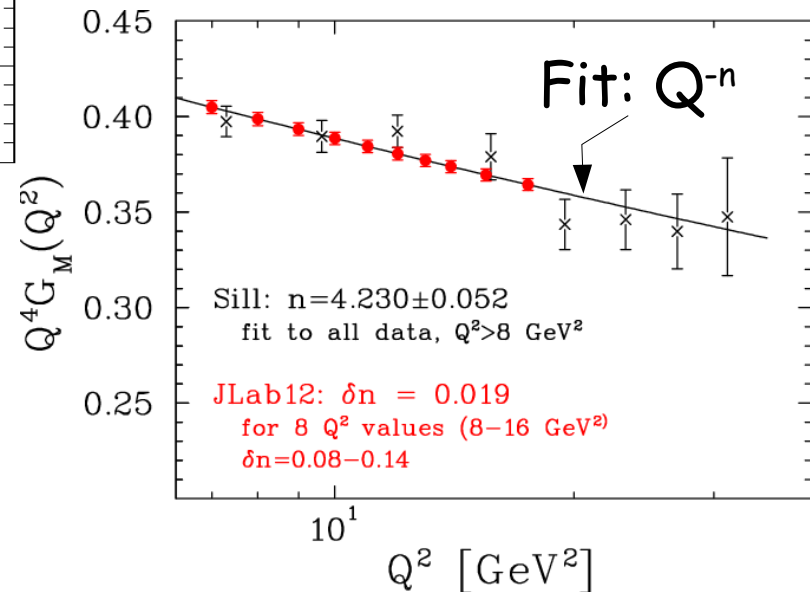


Precision Study of Q^2 Dependence



How does G_M^p approach the pQCD limit?

Onset of Scaling Behavior
at $Q^2 \sim 7-8 \text{ GeV}^2$?



Kinematics

- 3 Beam Energies
I = 80μA

- Both HRSs in
symmetric
configuration*

- 3 Redundant Q^2
• Different ε

- 21.5 days for LH_2

- 31 days requested

E_{beam}	Q^2	θ	E'	ε	Hours	Events
6.6	7.0	35	2.87	0.62	1	40k
	8.0	42	2.35	0.51	3	40k
	9.0	52	1.78	0.37	12	40k
	10.0	67	1.25	0.23	38	40k
8.8	9.0	29	4.00*	0.67	3	40k
	10.0	33	3.47*	0.59	9	40k
	11.0	38	2.95	0.51	11	40k
	12.0	44	2.42	0.41	27	40k
	13.0	53	1.86	0.30	67	28k
11	13.0	31	4.07*	0.58	21	28k
	14.0	35	3.53*	0.50	39	24k
	15.5	42	2.74	0.39	53	20k
	17.5	58	1.69	0.21	271	16k



Kinematics

Update for the PAC35 presentation

- 3 Beam Energies
I = 80μA

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• Different ϵ

- 21.5 days for LH_2

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E_e (GeV)	Q^2 (GeV) ²	θ_e (deg)	E' (GeV)	ϵ	Rate (Hz)	Time (hours)	Events
4.8**	7.0	71.0	1.08	0.25	0.60	9.3	40k
6.6	7.0	35.4	2.87	0.62	7.45	0.7	40k
6.6	8.0	42.0	2.35	0.51	2.29	2.4	40k
5.8**	9.0	77.0	1.00	0.18	0.15	36.3	40k
6.6	9.0	52.0	1.78	0.37	0.48	11.6	40k
8.8	9.0	29.3	4.00*	0.67	3.38	3.3	40k
6.6	10.0	67.0	1.25	0.23	0.15	38.3	40k
8.8	10.0	33.3	3.47*	0.59	1.31	8.5	40k
8.8	11.0	38.0	2.95	0.51	0.53	10.5	40k
8.8	12.0	44.0	2.42	0.41	0.21	26.7	40k
8.8	13.0	53.0	1.86	0.30	0.06	67.4	28k
11.0	13.0	31.3	4.07*	0.58	0.36	21.2	28k
11.0	14.0	35.0	3.54*	0.50	0.17	39.0	24k
11.0	15.5	42.0	2.74	0.39	0.053	52.8	20k
11.0	17.0	53.0	1.94	0.26	0.013	175.2	16k
						503.3	



Kinematics

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11.0	14.0	35.0	3.54*	0.50	0.17	39.0	24k

24 days



Systematic Uncertainties

Point to Point

Source	$\Delta\sigma/\sigma$ [%]
Incident Energy	0.3
Scattering Angle	0.1 (0.5)
Incident Beam Angle	0.1 (0.5)
Radiative Corrections	0.3
Beam Charge	0.3
Target Density Fluctuations	0.2
Spectrometer Acceptance	0.4 (0.8)
Endcap Subtraction	0.1
Detector Efficiencies and Dead Time	0.3
Sum in quadrature	0.8 (1.2)

Normalization

Source	$\Delta\sigma/\sigma$ [%]
Beam Charge	0.4
Target Thickness/Density	0.5
Radiative Corrections	0.4
Spectrometer Acceptance	0.6 (1.0)
Endcap Subtraction	0.1
Detector Efficiencies and Dead Time	0.4
Sum in quadrature	1.0(1.3)

$\Delta E/E = 1 \times 10^{-3} \Rightarrow \sim 0.70\%$ in $\Delta\sigma$

$\Delta\theta = 1 \text{ mrad} \Rightarrow \sim 0.75\%$ in $\Delta\sigma$

Statistics: 0.5 - 0.8%

TOTAL (Scale + Rand. + Stat.) : 1.3 (1.8) % **Goal: 2% or better**

Lower numbers indicate values estimated if PAM device functions as well as desired



Beam Energy

Require use of eP and Upgrade of Arc energy methods for JLab 12 GeV

Precision $\sim 3\text{-}4 \times 10^{-4}$

Monitor stability and energy spread with

- OTR
- Tiefenback
- Synchrotron Light Interferometer (SLI)

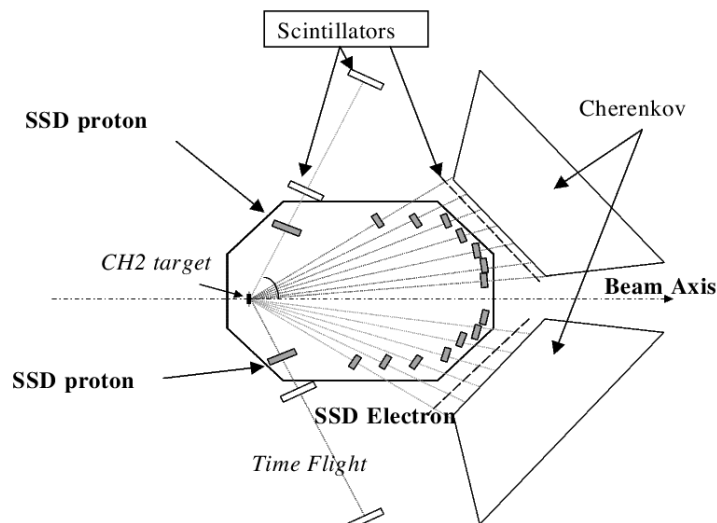


Figure from Alcorn et al. NIM A522 (2004)

Bryan Moffit
PAC32 Presentation

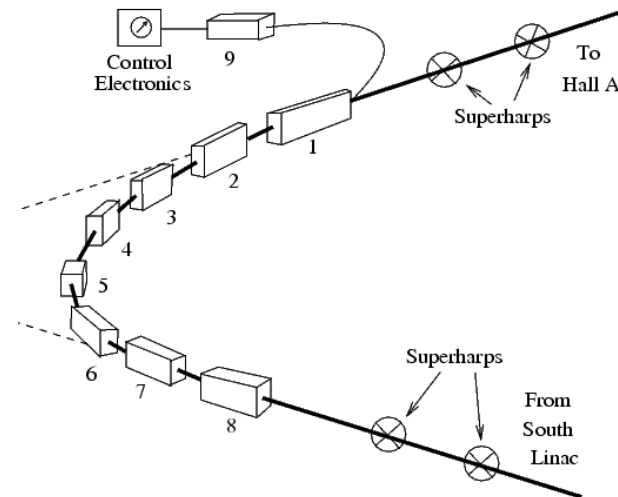


Figure from Kevin Kramer Ph.D. Thesis (2003)



Target Configuration

LH₂ : 20 cm Racetrack

- Vertical Flow Design
- Dedicated Studies of density stability
- Luminosity Monitor in datastream

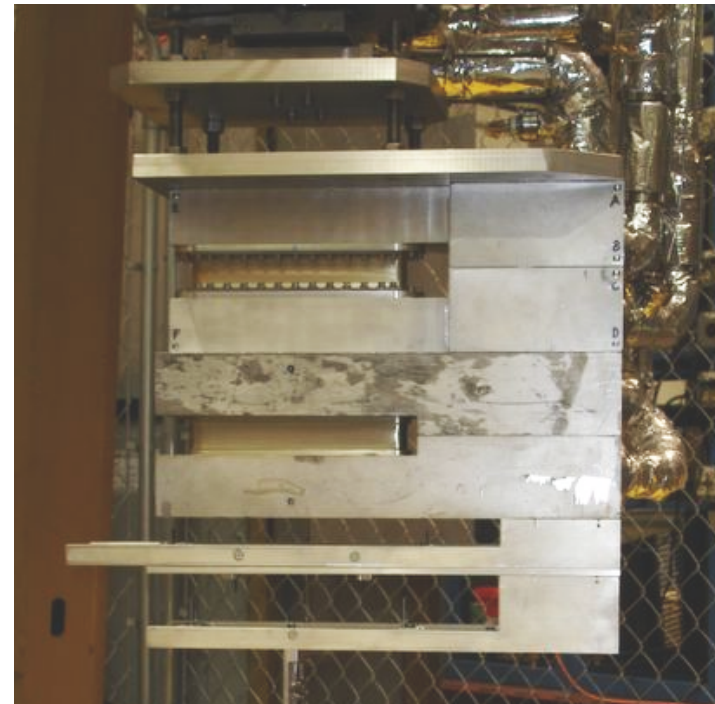
Solid Aluminum Foils (Dummy)

- Endcap subtraction

Carbon Optics Targets

- 1-2 cm spacing along z_{lab}
for extended target
optics/acceptance

Solid Target / Racetrack Endcaps measured with X-ray attenuation



Picture from 2005 HAPPEX-II

HRS Detector Package

Main Trigger (electrons)

- S2m AND Gas Cherenkov

Secondary Triggers

- S0 AND Gas Cherenkov
- S0 AND S2m

Gas Cherenkov with Lead Glass Counters

- 10^4 pion rejection ?
- 99.5% electron efficiency

Additional VDC layer

- Improvement in tracking efficiency
- Reduction of non-statistical tails

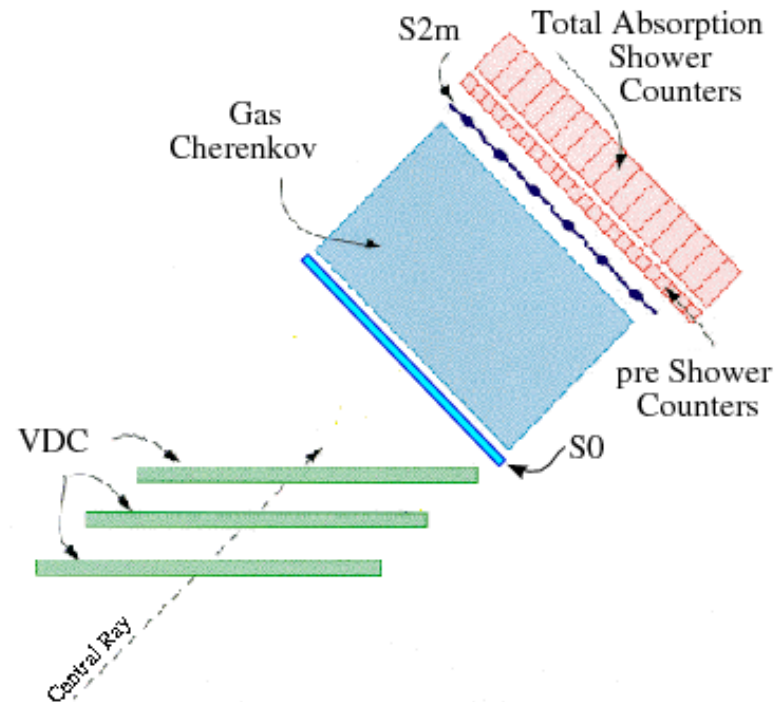


Figure from Hall A Webpage (modified)

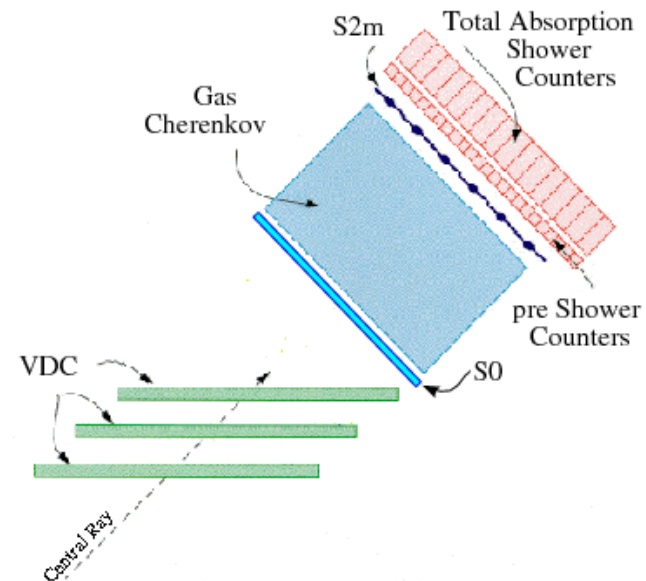
Additional Wire Chamber

Current usage:

- Tight cuts on # hits/chamber
- Correct for lost events
- 0.5% correction on σ_{ep} for E01-001

One additional Wire Chamber for each spectrometer

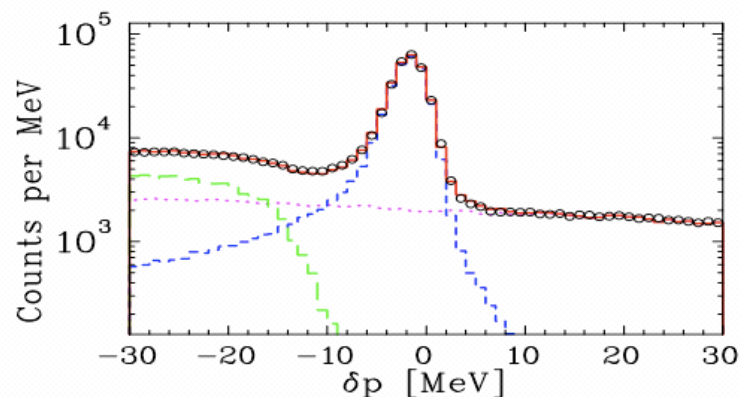
- Added redundancy to account of multiple hit clusters per event.
- Higher tracking efficiency



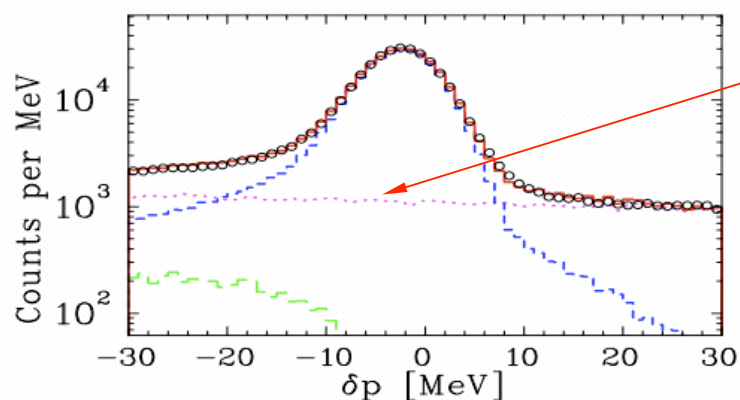
Additional Wire Chamber Options:

- ★ Use "Spare" and build another "spare" from on-site components
- ★ Use Multi-Wire Drift Chambers from BigBite Spectrometer
- ★ Use front drift chambers from Focal Plane Polarimeter

Spectra from the Super Ratio experiment



tions where the electron was detected. We also require a single clean cluster of hits in each drift chamber plane to avoid events where the resolution is worsened by noise in the chambers. This reduces the non-Gaussian tails, but leads to an inefficiency of roughly 7%, with a small (0.25%) ε dependence, possibly related to the variation of rate with ε . We correct the yield for the observed inefficiency and apply a 100% uncertainty on the ε dependence of the correction.

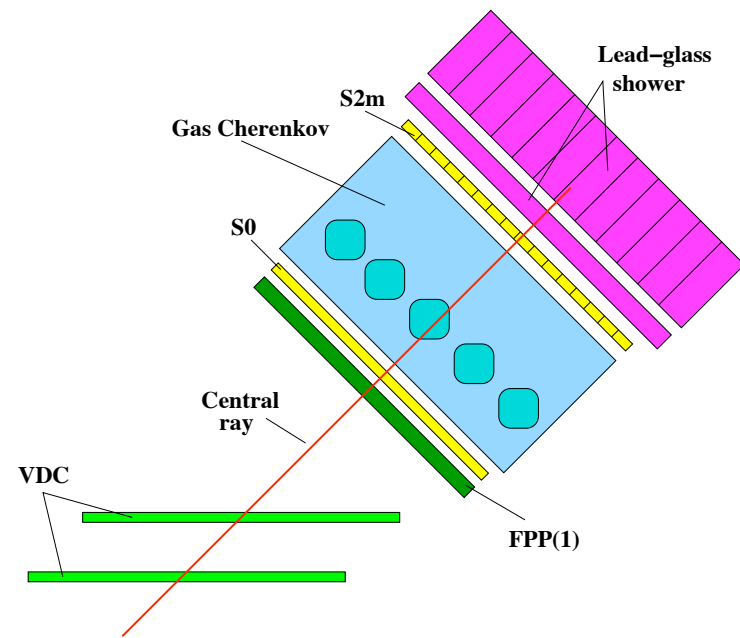
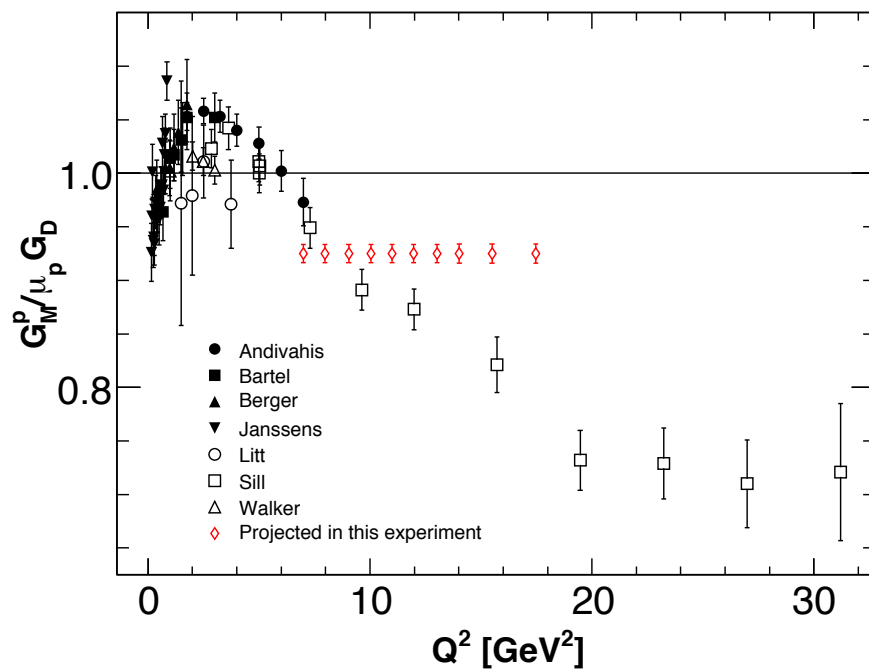


background

FIG. 1 (color online). The measured δp spectrum for the low (top) and high (bottom) ε points at $Q^2 = 3.2 \text{ GeV}^2$ (circles). The dotted magenta line is the background from the target walls, the long-dash green line is the simulated background from $\gamma p \rightarrow \pi^0 p$ and $\gamma p \rightarrow \gamma p$ reactions, the short-dash blue line is the simulated elastic spectrum, and the solid red line (largely obscured by the data points) is the sum of the target wall, elastic, and background contributions.

E12-07-108 (GMp)

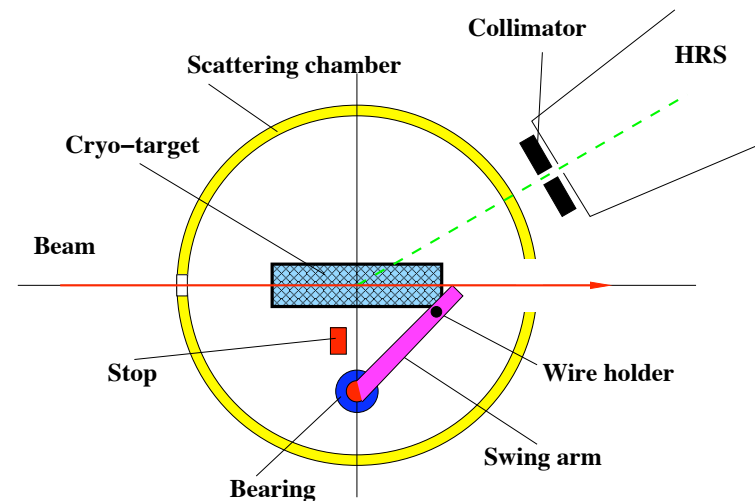
- It is the only one measurement of the cross section – key input to all form factors and many other experiments
- It was proposed in 2007 after the GEp(5) was formulated
- It is based on the 15-years success of HRS



E12-07-108 (GMp)

Source	$\Delta\sigma/\sigma$ (%)
Point to point uncertainties	
Incident Energy	<0.3
Scattering Angle	0.1–0.3
Incident Beam Angle	0.1–0.2
Radiative Corrections*	0.3
Beam Charge	0.3
Target Density Fluctuations	0.2
Spectrometer Acceptance	0.4–0.8
Endcap Subtraction	0.1
Detector efficiencies and dead time	0.3
<i>Sum in quadrature</i>	<i>0.8–1.1</i>
Normalization uncertainties	
Beam Charge	0.4
Target Thickness/Density	0.5
Radiative Corrections*	0.4
Spectrometer Acceptance	0.6–1.0
Endcap Subtraction	0.1
Detector efficiencies and dead time	0.4
<i>Sum in quadrature</i>	<i>1.0–1.3</i>
<i>Statistics</i>	<i>0.5–0.8</i>
Total (Scale+Rand.+Stat.)	1.2–1.7

Several parameters need serious work on systematic, among them: the scattering angle, detector/DAQ efficiency, HRS solid angle, the target density, the beam charge



GMP and DVCS

GMP: 20 cm x 80 μ A

$L = 4.3 \times 10^{38}$ Hz/cm²

both HRSs x 24 days
~ 200 HRS-day x 10^{38}

Q^2 (GeV ²)	k (GeV)	x_{Bj}	$q'(0^\circ)$ (GeV)	D (m)	θ_q (deg)	θ_{calo}^{min} (deg)	t_{min} (GeV ²)	t_{max} (GeV ²)	$\sigma(M_X^2)$ (GeV ²)	$\mathcal{L}/10^{38}$ (cm ⁻² /s)	HRS	DVCS	Time (days)
3.0	6.6	0.36	4.35	1.5	11.7	7.1	-0.16	-0.42	0.23	0.75	479	1.16	3
4.0	8.8	0.36	5.83	2.0	10.3	7.0	-0.17	-0.42	0.26	1.3	842	1.74	2
4.55	11.0	0.36	6.65	2.5	10.8	7.0	-0.17	-0.42	0.27	2	2460	4.63	1
3.1	6.6	0.5	3.11	1.5	18.5	11.0	-0.37	-0.64	0.17	0.75	873	0.77	5
4.8	8.8	0.5	4.91	2.0	14.5	8.9	-0.39	-0.70	0.20	1.3	716	0.82	4
6.3	11.0	0.5	6.50	2.5	12.4	7.9	-0.40	-0.72	0.20	2.	778	0.99	4
7.2	11.0	0.5	7.46	2.5	10.2	7.0	-0.40	-0.75	0.25	2.	331	0.53	7
5.1	8.8	0.6	4.18	1.5	17.8	10.4	-0.65	-1.06	0.16	0.75	338	0.27	13
6.0	8.8	0.6	4.97	2.0	14.8	9.2	-0.67	-1.05	0.18	1.3	227	0.22	16
7.7	11.0	0.6	6.47	2.5	13.1	8.6	-0.69	-1.10	0.20	2.	274	0.28	13
9.0	11.0	0.6	7.62	3.0	10.2	7.3	-0.71	-1.14	0.22	3.	117	0.17	20

E_e (GeV)	Q^2 (GeV) ²	θ_e (deg)	E' (GeV)	ϵ	Rate (Hz)	T (hours)	
4.8**	7.0	71.0	1.08	0.25	0.60	9.3	40k
6.6	7.0	35.4	2.87	0.62	7.45	0.7	40k
6.6	8.0	42.0	2.35	0.51	2.29	2.4	40k
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6.6	9.0	52.0	1.78	0.37	0.48	11.6	40k
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6.6	10.0	67.0	1.25	0.23	0.15	38.3	40k
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8.8	12.0	44.0	2.42	0.41	0.21	26.7	40k
8.8	13.0	53.0	1.86	0.30	0.06	67.4	28k
11.0	13.0	31.3	4.07*	0.58	0.36	21.2	28k
11.0	14.0	35.0	3.54*	0.50	0.17	39.0	24k

8.8 GeV ~ 5 days; 11 GeV ~ 2.5 days

DVCS in E03-106: $L = 4. \times 10^{37}$ Hz/cm²

DVCS: $L = 15$ cm x J μ A
 $0.75\text{-}3 \times 10^{38}$ Hz/cm²

$L/L_{GMP} \times T$ at 6.6 GeV ~ 1.4 days

$L/L_{GMP} \times T$ at 8.8 GeV ~ 8.6 days

$L/L_{GMP} \times T$ at 11 GeV ~ 21 days

Threshold inelastic electron scattering from the proton at high momentum transfers

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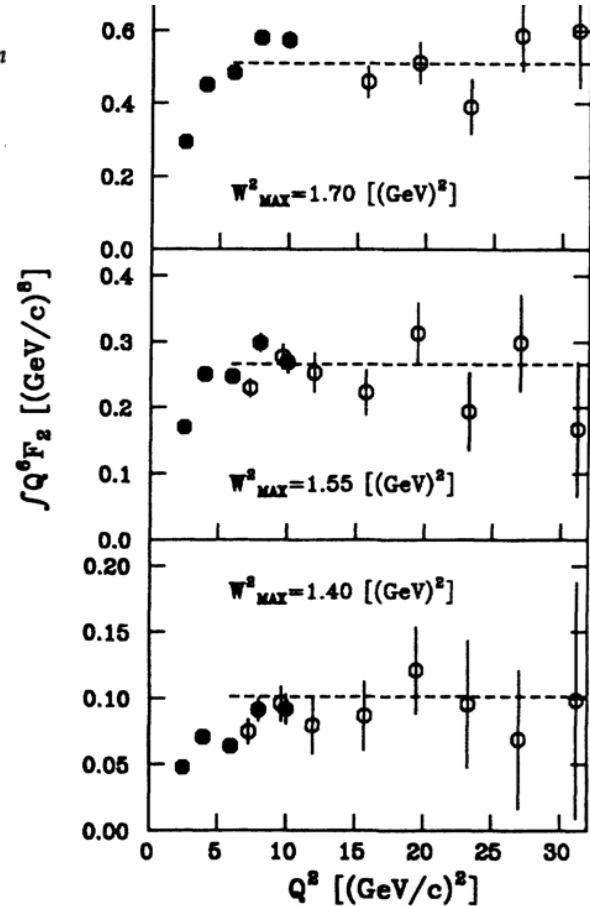
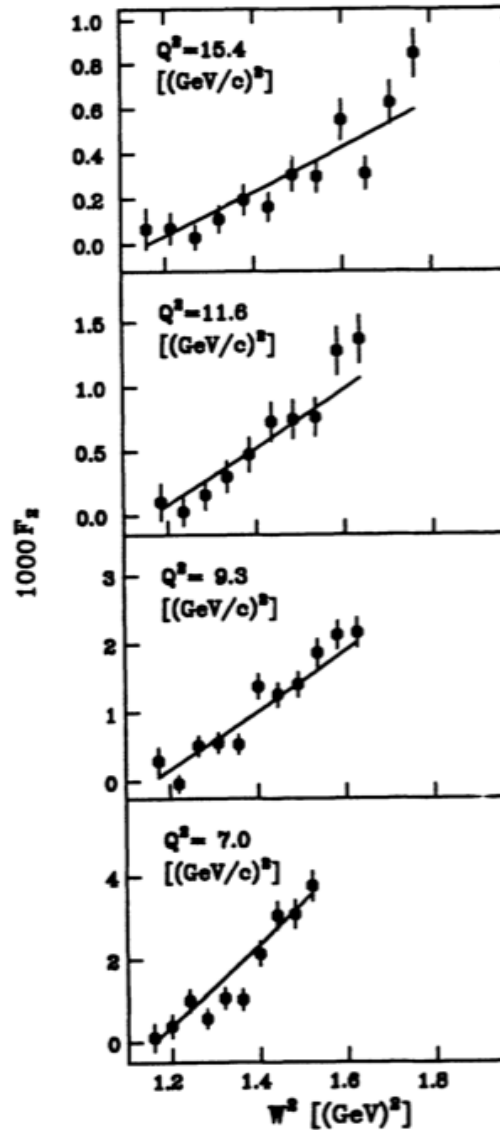
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QCD firm prediction
for the threshold pion
electro-production:

$$Q^6 F_2 = \text{const}$$



The integrated values of $Q^6 F_2(x, Q^2)$ from t_1 to t_2 (from 6 $(\text{GeV})^2$ to the maximum values indicated in the panels, as a function of Q^2 . The open circles represent the integrated values from 6 $(\text{GeV})^2$ to W^2_{MAX} .