

# Neutron Extraction: A First Approach

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  - $E = 4.74$  GeV
  - $E = 5.89$  GeV
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# Overview

In order to extract **neutron** information from  ${}^3\text{He}$ :

- Use polarizations of **neutron** and **proton**
- Correct for **off-shell nucleon spin structure functions**
- Use several models to compute  $g_1^p$  and  $g_2^{p,WW}$
- Models used:
  - **DSSV** - Phys.Rev.Lett.101:072001,2008
  - **BB** - hep-ph/0203155
  - **DNS2005** - D.de Florian, G.A. Navarro, and R. Sassot, Phys. Rev. D71 (2005) 094018.
  - **GS** - T. Gehrmann and W.J. Stirling, Phys.Rev. D53 (1996) 6100.
- **NOTE:**
  - $g_2^p = g_2^{p,WW}$
  - Neutron corrections valid for **DIS** region only ( $x \lesssim 0.5 - 0.6$ )

# $^3\text{He}$ Correction

Calculate  $g_1^n$  and  $g_2^n$  from equations 1 and 2

$$g_1^{^3\text{He}} = (P_n + 0.056) g_1^n + (2P_p - 0.014) g_1^p \quad (1)$$

$$g_2^{^3\text{He}} = (P_n + 0.056) g_2^n + (2P_p - 0.014) g_2^{p,WW} \quad (2)$$

where:

- $g_1^{^3\text{He}}$  and  $g_2^{^3\text{He}}$  are E06-014 data
- $g_1^p$  and  $g_2^{p,WW}$  are calculated from 4 models
- $P_n = 0.86 \pm 0.02$  (neutron polarization)
- $P_p = -0.028 \pm 0.004$  (proton polarization)
- **0.056** and **-0.014** come from off-shell nucleon corrections (See Xiaochao Zheng thesis)

# Polarized Structure Functions: $g_1$

4.74 GeV

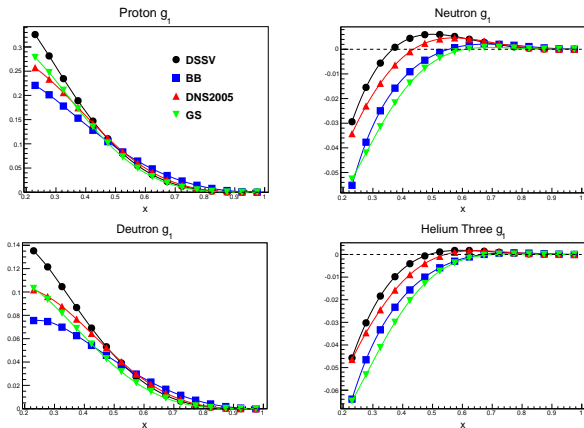


Figure: Each of the four models results for the proton, neutron, deuteron and helium three  $g_1$  polarized structure function at beam energy of 4.74 GeV and E06-014  $x$  and  $Q^2$  values.

Polarized Structure Functions:  $g_2^{WW}$ 

4.74 GeV

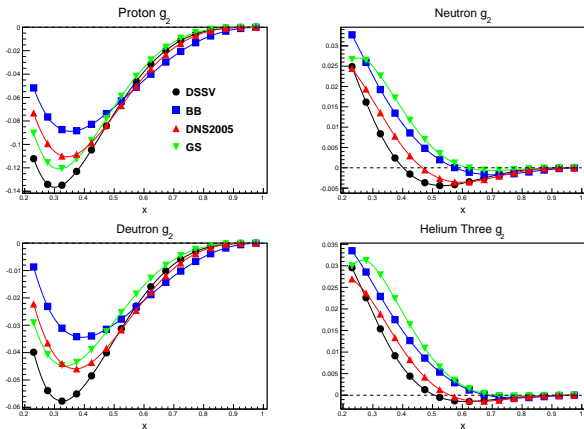
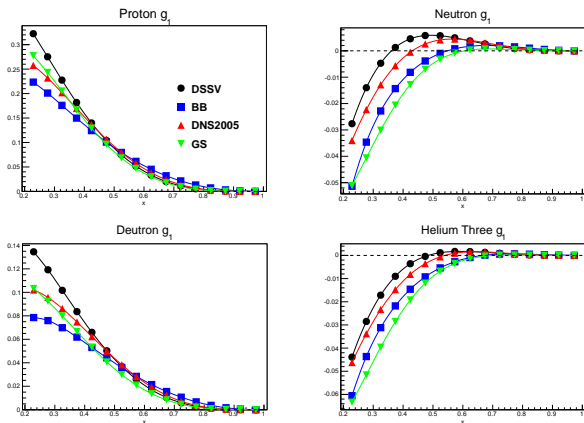


Figure: Each of the four models results for the proton, neutron, deuteron and helium three  $g_2^{WW}$  polarized structure function at beam energy of 4.74 GeV and E06-014  $x$  and  $Q^2$  values.

# Polarized Structure Functions: $g_1$

5.89 GeV



**Figure:** Each of the four models results for the proton, neutron, deuteron and helium three  $g_1$  polarized structure function at beam energy of 5.89 GeV and E06-014  $x$  and  $Q^2$  values.

# Polarized Structure Functions: $g_2^{WW}$

5.89 GeV

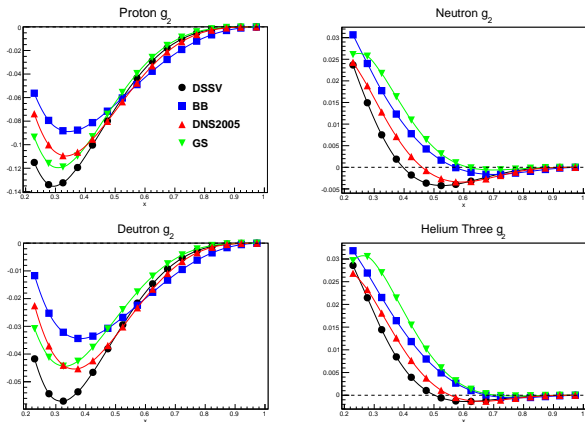


Figure: Each of the four models results for the proton, neutron, deuteron and helium three  $g_2^{WW}$  polarized structure function at beam energy of 5.89 GeV and E06-014  $x$  and  $Q^2$  values.



# Nuclear Correction Size

4.74 GeV

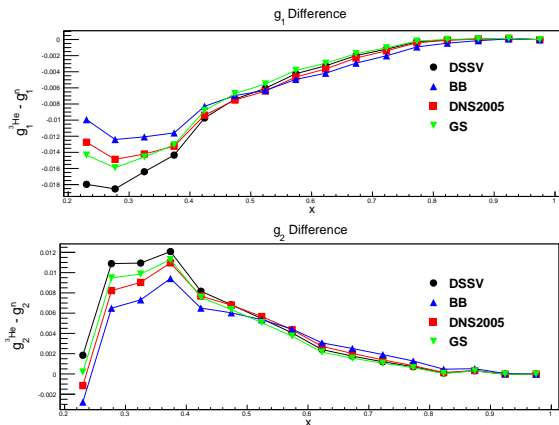


Figure: The difference between the <sup>3</sup>He and extracted neutron structure functions are shown as a function of x at a beam energy of 4.74 GeV.

# Nuclear Correction

4.74 GeV

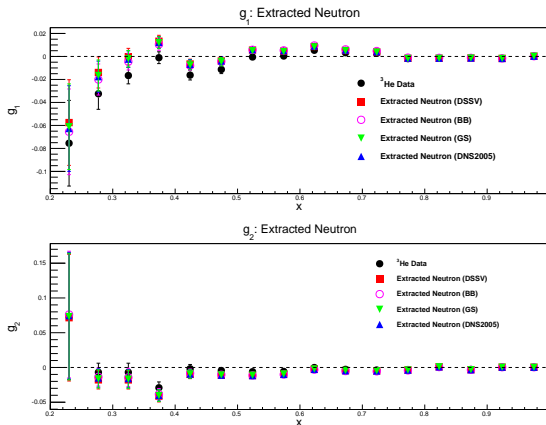


Figure: Plotted are the polarized structure function results to the neutron extraction using the defined method compared to the <sup>3</sup>He polarized structure functions at E = 4.74 GeV. All uncertainties are from <sup>3</sup>He statistical uncertainties.

# Nuclear Correction Size

5.89 GeV

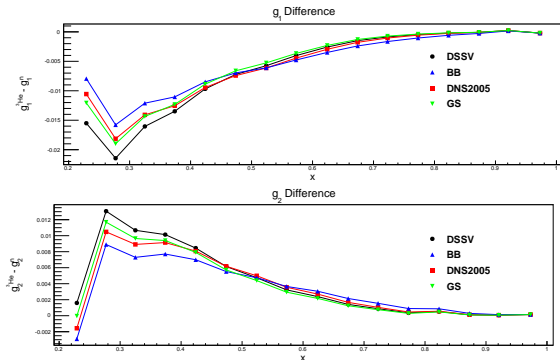


Figure: The difference between the  $^3\text{He}$  and extracted neutron structure functions are shown as a function of  $x$  at a beam energy of 5.89 GeV.

# Nuclear Correction

5.89 GeV

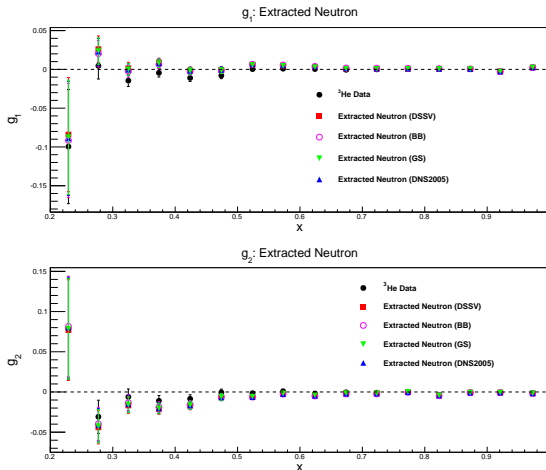


Figure: Plotted are the polarized structure function results to the neutron extraction using the defined method compared to the  $^3\text{He}$  polarized structure functions at E = 5.89 GeV. All uncertainties are from  $^3\text{He}$  statistical uncertainties.

# Systematic Uncertainty Contributions

The following uncertainties contribute to the total uncertainty:

- Neutron and proton polarizations
- Dependence from **all** models
- Dependence on a **single** model

The **first two** contributions are considered here

# Polarization Uncertainties

The uncertainty from the neutron and proton polarization are given by:

$$(\delta g_1^n)_{P_p}^2 = \left( \frac{2g_1^p}{P_n + 0.056} \delta P_p \right)^2 \quad (3)$$

$$(\delta g_1^n)_{P_n}^2 = \left( \frac{g_1^{3He} - (P_p - 0.014)g_1^p}{(P_n + 0.056)^2} \delta P_n \right)^2 = \left( \frac{g_1^n}{P_n + 0.056} \delta P_n \right)^2 \quad (4)$$

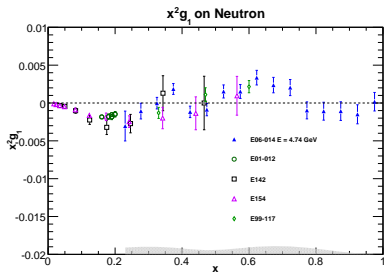
$$(\delta g_1^n)_{Pol} = \sqrt{(\delta g_1^n)_{P_p}^2 + (\delta g_1^n)_{P_n}^2} \quad (5)$$

- Similar for  $g_2^n$ , with  $g_1^n \rightarrow g_2^n$ ,  $g_1^p \rightarrow g_2^{p,WW}$  and  $g_1^{3He} \rightarrow g_2^{3He}$
- Each model gave **similar uncertainties**, so they were **averaged** together for each x bin.

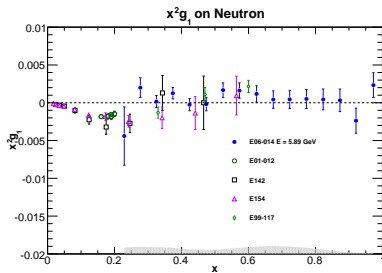
# Model Difference Uncertainty

Assign an uncertainty based on **difference** between the 4 models

- Computed the difference of  $g_1^n$  and  $g_2^n$  from each of the models (i.e.  $|g_1^n_{DSSV} - g_1^n_{GS}|$ )
- The differences varied in size between the models, so **largest difference** was taken as the uncertainty for each x-bin
- **Total systematic uncertainty** is quadrature sum of the **model difference** and **polarization** uncertainties
- Total systematic uncertainty approximately **order of magnitude smaller** than statistical error.



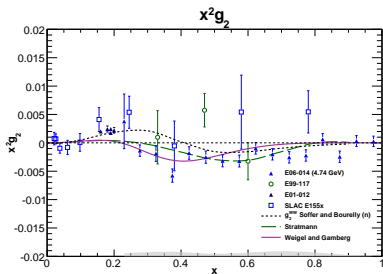
(a) 4.74 GeV



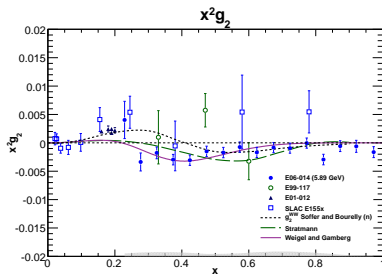
(b) 5.89 GeV

Figure: Preliminary  $g_1^n$  results for 4 and 5 pass data. The gray band represents the systematic uncertainty currently assigned to the neutron extraction. Note that these results are only valid up to  $x = 0.5$  in the 4.74 GeV data and  $x = 0.6$  in the 5.89 GeV data.





(a) 4.74 GeV



(b) 5.89 GeV

Figure: Preliminary  $g_2^n$  results for 4 and 5 pass data. The gray band represents the systematic uncertainty currently assigned to the neutron extraction. Note that these results are only valid up to  $x = 0.5$  in the 4.74 GeV data and  $x = 0.6$  in the 5.89 GeV data.

# Summary

- All 4 models lead to similar polarized neutron structure functions
- Good agreement with world data
- For second approach:
  - Integrate Wally's neutron extractions
  - Correct resonance region corrections
  - Apply single model dependence (?)

# To Do

- Form and fit LHRS, BB, CLAS and E142  $e^+/e^-$  ratios to use for pair-production dilution factor
- Closer look at implementing bad preshower block in GEANT4
- Study distributions of  $\pi^{+/-}$  and  $e^{+/-}$  in BigBite
- Apply Wally's neutron corrections